Demonstration of Visible and Near Infrared Raman Spectrometers and Improved Matched Filter Model for Analysis of Combined Raman Signals

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DEMONSTRATION OF VISIBLE AND NEAR INFRARED RAMAN SPECTROMETERS
AND IMPROVED MATCHED FILTER MODEL FOR ANALYSIS OF COMBINED RAMAN
SIGNALS

by

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B.S.E.E. December 2017, Old Dominion University

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ABSTRACT

DEMONSTRATION OF VISIBLE AND NEAR INFRARED RAMAN SPECTROMETERS AND IMPROVED MATCHED FILTER MODEL FOR ANALYSIS OF COMBINED RAMAN SIGNALS

Alexander Matthew Atkinson
Old Dominion University, 2019
Director: Dr. Hani E. Elsayed-Ali

Raman spectroscopy is a powerful analysis technique that has found applications in fields such as analytical chemistry, planetary sciences, and medical diagnostics. Recent studies have shown that analysis of Raman spectral profiles can be greatly assisted by use of computational models with achievements including high accuracy pure sample classification with imbalanced data sets and detection of ideal sample deviations for pharmaceutical quality control. The adoption of automated methods is a necessary step in streamlining the analysis process as Raman hardware becomes more advanced. Due to limits in the architectures of current machine learning based Raman classification models, transfer from pure to mixed sample analysis is not possible.

This thesis presents the design, fabrication, and data collected from two different Raman spectrometers, a visible light system operating at 532 nm and a near infrared system operating at 785 nm. For each system, the optical design and operational theory of the main components will be explained. Data collected on each system will then be presented. Additionally, a learned matched filter computer model was developed to analyze Raman line profiles and can detect the signatures of multiple materials in a single data point. The presented model incorporates machine learning theory into the traditional matched filter model for higher probability of detection and much reduced probability of false alarm. The structure and operation of the model will be explained, and analysis of both real and simulated mixed-sample Raman spectra will be presented.
Copyright, 2019, by Alexander Matthew Atkinson, All Rights Reserved.
Gutta cavat lapidem.

This thesis is dedicated to my family, advisors, and friends who never let me give up.
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CHAPTER 1
INTRODUCTION

Raman spectroscopy is a powerful material analysis technique that can provide insight into the composition of solid, liquid, and gaseous samples by measuring the frequency shift of inelastically scattered light from a monochromatic source.\(^1\) Technologies developed since its discovery have made Raman spectroscopy an analysis standard with applications in fields ranging from interplanetary exploration to medical diagnostics and pharmaceutical quality control.\(^2\)-\(^4\) As advancements have been made in the field, Raman systems have gained a need for rapid data analysis techniques capable of matching the fast acquisition times that have been achieved, lower potential for human error, and open Raman spectroscopy as an analysis technique to a wider variety of users. Planetary science fields are actively researching data analysis techniques that can handle the large amount of complex science that interplanetary missions will collect.\(^2\)

Machine learning has proven itself to be a powerful tool for discriminating between Raman spectra. Recent studies have achieved high accuracies in high-class single sample classification problems and binary classification of complex samples such as human blood.\(^5\),\(^6\) Although past studies have established a generalized scheme for accurate classification of Raman spectra, the current state of machine learning and Raman has a need for a model which can analyze mixed samples. While sample refinement may be possible in a laboratory environment, in-situ Raman instruments may not be able to physically isolate samples from each other due to restrictions from the environment or improper equipment.

The journal model used for this thesis is *Optical Engineering*. 
In machine learning, cases in which class labels are not mutually exclusive place restrictions on the type of model that can be used. Models that attempt to solve these problems need to be able to detect multiple classes in a single input. When brought into the scope of Raman spectroscopy an appropriate model would ideally be used to inform the user what components are likely to make up a mixed sample by comparing features present in an input data point with specific spectral patterns that the model learned to associate with materials during training. This chapter introduces the problem of detecting multiple classes simultaneously in the context of Raman spectroscopy. In it, the flaws inhibiting this capability in current models used for Raman analysis will be explained and one possible solution will be introduced.

1.1 Raman spectroscopy

Raman spectroscopy is a vibrational spectroscopic technique that analyzes the frequency shift of inelastically scattered light that is emitted when a Raman-active sample is struck with a monochromatic light source. Upon exposure to an electric field, the molecules in a sample deform and begin to vibrate effectively transforming into oscillating dipoles. The characteristic Raman signature of a Raman-active sample is based upon vibrational modes induced by that dipole which cause a change in the molecule’s polarizability.

The likelihood of a photon being inelastically scattered is much lower than that of elastic (Rayleigh) scattering. Because of this, Raman spectrometers typically incorporate high optical density filters at the laser line to make Raman scattered light detectable. Raman scattering can cause the wavelength of incident light to become longer or shorter, referred to as “Stokes” and “anti-Stokes” scattering respectively. The Maxwell-Boltzmann distribution law predicts that molecules are more likely to be in a ground state causing Stokes scattering to be more common and “brighter” relative to
anti-Stokes. When multiple Raman-active molecules are struck by the same incident a combination of spectral features can appear on the line profile.\textsuperscript{2}

Figure 1 shows Raman spectra from pure sulfur (Figure. 1A), pure naphthalene (Figure. 1B), and a mixed sample comprised of both materials (Figure. 1C).\textsuperscript{10} It can be seen in Figure. 1C that spectral peaks from both naphthalene and sulfur appear in the mixed sample’s line profile. Recently designed machine learning models that show high classification accuracy with pure samples will not be
able to transfer to mixed sample analysis due to limitations of some architectural components.\textsuperscript{11} While training a model with data collected from all different combinations of pure samples is a possible solution, the amount of training data which would need to be collected to train a model in that way would increase exponentially as more materials were added to the dataset. This leaves a need for an alternative method that can detect multiple materials in a single line profile after being trained with pure sample data.

1.2 Current Methods for Automated Analysis of Raman spectroscopy

Modern papers concerning automated analysis of Raman spectra are increasingly incorporating machine learning techniques as their algorithms of choice.\textsuperscript{4-6} Liu et al. offers the broadest investigation to date into the effectiveness of different machine learning models at classifying pure sample Raman data.\textsuperscript{5} In their research, a total of 7 classifiers and 6 baseline correction methods were tested for classification accuracies of an unbalanced dataset created from several mineral Raman spectra databases provided by the RRUFF\textsuperscript{†} project.\textsuperscript{14} It was found that the convolutional neural network (CNN) consistently showed the highest accuracy across all baseline correction techniques, achieving a peak classification accuracy of just over 96%.

The CNN is a class of deep learning network which was designed for image processing and classification tasks.\textsuperscript{15} CNNs traditionally utilize a single image input layer with multiple convolutional layers following a shared-weight architecture.\textsuperscript{16} These types of networks were originally inspired by biology, specifically by the visual processing systems of animals.

CNNs gained their name from their usage of the convolution operation. The purpose of the convolutional step is to allow the network to learn to associate specific features with certain classes and to also scale down high-dimensional inputs to decrease computational load. Compared to a traditional

\textsuperscript{†} - RRUFF is not an acronym. It is the official name of the project which maintains the public access Raman databases that were used for part of the model verification in this thesis.
neural network, the CNN’s learnable features typically consist of a set of filters in each convolutional layer along with one fully connected layer for output. Each filter is spatially small with respect to the input image and is used to compute convolutions by performing dot products as they are swept across the layer’s input as illustrated in Figure 2.

While CNNs have achieved high accuracy classification with pure sample Raman data, they will fail when tasked with detecting multiple Raman classes in a single input just as they do in image processing applications. Although Raman spectral data avoids the orientation encoding problem, simply because all line profiles will begin and end at the same points, it is still susceptible to misclassification due to the model not learning features’ relative positions to each other. This loss of spatial encoding in CNNs is traceable to the use of max pooling layers which scale down an input vector or matrix by selecting only the largest numeric value to be passed forward.
The other main issue inherent in models currently being used for Raman classification arises when the training dataset consists of only pure sample Raman spectra. Figure 3 shows the input weights of a trained softmax layer (SML) for classification of naphthalene and sulfur Raman spectra.\textsuperscript{17} Figures 3A and 3C show all baseline corrected training observations for naphthalene and sulfur respectively. Figures 3B and 3D show the input weights of the naphthalene and sulfur output nodes respectively. As would be expected, each output neuron learned to “pay attention” to locations of the line profile where Raman peaks of their respective pure sample are found, seen by the positive weights learned in those regions. Along with this, however, both output neurons also learned to apply negative weights to regions of the line profile where features are found in the other pure sample, effectively assuming mutual exclusivity between spectral features. Due to the lack of training observations containing spectral features from both samples, the SML assumes that it will never see an input containing spectral features from both samples. When presented a line profile with spectral features from all learned pure samples, the dot product of the input with both weight vectors would approach the negative bias of their respective output neuron making simultaneous detection impossible.

1.3 Classification with Matched Filters

Structurally, the model presented in this thesis closely resembles a matched filter. In a matched filter, detection of each class’ spectral features is accomplished on a singular basis. For discrete signals, a matched filter is generated from the complex conjugate of a known sample signal.\textsuperscript{18} In this case, because Raman signals are entirely real, the filter for each class can be generated by calculating the mean signal across all reference datapoints.\textsuperscript{18} Once all class filters have been calculated, classification
Figure. 3. Pure naphthalene and pure sulfur training data (A & C) and the learned input weights for a softmax layer (B & D). It can be seen that the learned weights for the naphthalene and sulfur output neurons adjusted to increase sensitivity to the presence of spectral features from their respective material. Figure. 3B, for example, has positive weights from input neurons that commonly line up with naphthalene peaks.

can be performed by calculating the correlation coefficients between the input signal and all class filters. If the correlation coefficient between the input signal and a class filter is high enough, it is counted as a hit. Hypothetically, utilizing machine learning for the generation of class filters would allow for a higher degree of differentiation between spectral features in and out of its class.
1.4 Research Objectives

Advancements in Raman spectrometer hardware have allowed for compact instruments to have deployment capabilities directly on interplanetary missions, flexible usage conditions requiring no sample collection/preparation, and no need for daylight radiation shielding.\(^2\) As the science that can be collected from a Raman spectrometer in a given amount of time increases, a bottleneck will be created in data analysis which leaves a need for a faster method of spectral data classification. Although recent studies have achieved high classification accuracies with large databases of pure samples, these models are unable to be directly transferred classification of complex signals that will be found on interplanetary missions.

The objective of this research was to design, build, and test two different Raman instruments and to develop a computerized model that can automatically analyze large amounts of data. Both instruments are remote in their operation and utilize state of the art optical hardware. One system operates in the visible light spectrum with a laser wavelength of 532 nm, and the other operates in the near infrared (NIR) spectrum with an incident of 785 nm. The visible system uses a powerful 45 mJ Q switched laser and performs well for mineral analysis. The NIR system utilizes a lower energy pulsed laser at a longer wavelength to reduce laser induced fluorescence. The model is based off a matched filter and is capable of detecting Raman signatures from multiple different materials in a single line profile while only using pure sample data for training. Instead of utilizing a mean class signal for a filter, however, the filters are learned through the process of training multiple, class specific feedforward neural networks (FNNs). Each FNN in the model will be referred to as a sub-FNN because they are part of the larger model as a whole.
An example structure of a model for analysis of a two-species mixed sample can be seen in Figure 4. By utilizing a single FNN for the detection of each class, high accuracy detection of class-specific spectral features can be achieved. Each sub-FNN is tasked with analyzing sections of an input Raman line profile. The sections of the line profile associated with each sub-FNN are defined during training as the regions of the line profile where spectral features of the sub-FNN’s respective pure material (class) are found, labeled as Z1, Z2, and Z3 in Figure 4. Sub-FNN input restriction is performed as a type of feature selection to lower the computational load of having many FNNs working in parallel and to lower the risk of random noise or non-learned spectral features causing a false positive detection. In this thesis, the number of hidden units in each sub-FNN was kept constant. The output of the model is a
vector consisting of all sub-FNN activations. Ideally, if the model in Figure 4 analyzed the line profile in the same figure only the lower (dashed) sub-FNN would activate because spectral features are only present in the areas of the input layer that are being passed to it. Each element of the model output ranges from 0 to 1 inclusively and should be thought of as the similarity the sub-FNN’s input had to the data it was trained with (i.e. whether or not spectral features from a learned component material are present).

This model is capable of analyzing Raman spectra collected from multi-component samples without utilizing complicated while retaining high performance pure sample classification capabilities. To test the model, mass data was collected with the 532nm time resolved Raman spectrometer. The collected data was used to analyze both real mixed sample data as well as simulated mixed sample data created by generating random combinations of pure sample signals. Mineral Raman spectra datasets maintained by the RRUFF project were also used to generate more complex simulated mixed sample signals.
CHAPTER 2

532nm RAMAN SPECTROMETER

This chapter describes the hardware used to collect data for model verification. The data collection system is outlined in Figure 5 and consists of a Big Sky Laser UltraCFR serving as excitation source, a Kaiser Optical Systems Inc. (KOSI) Holospec f/1.8 spectrometer, and a Princeton Instruments PIMAX I ICCD camera.\textsuperscript{19-21} The operating concepts of the laser, receiver, camera, and system performance will be explained in the following sections.

![Block diagram of hardware setup for 532 nm system. System consists of a Big Sky Laser UltraCFR, a Kaiser Optical Systems Inc. (KOSI) Holospec f/1.8 spectrometer, and a Princeton Instruments PIMAX I ICCD camera.\textsuperscript{19-21} A custom receiver was made for optimal usage in a laboratory environment.](image-url)
2.1 Laser excitation source

An actively Q-switched Big Sky Laser (now Quantel) UltraCFR laser was used as the monochromatic excitation source for collection of the mixed sample Raman data and the 5-class pure sample dataset. A flash lamp induces lasing in the Nd:YAG media, emitting 1064 nm radiation. The IR light is then frequency doubled to 532 nm by a potassium titanyl phosphate (KTP) non-linear crystal housed in a separate oven module at the front of the laser for optimal temperature control. Light is emitted from the aperture in 8 ns long pulses. Pulse frequency was kept at 20 Hz for all data collection and the laser’s “Q-switch sync” output signal was used as the main trigger for intensifier-gated mode operation. Timing for gated mode operation will be explained in Section 2.3.

2.2 Receiver and spectrometer

Laser light is directed to the sample in co-axial geometry by a mirror and a 90° prism for optimal backscatter collection. Use of a prism was chosen over a dichroic due to the high energy per pulse (45 mJ at 532 nm). A 200mm biconvex lens focuses the incident laser onto the sample at normal incident and collects the backscattered signal. The collected signal is then resized and focused into the spectrometer by a 20x microscope objective for optimal overall throughput and high collimation in the spectrometer’s filter section. Inside the spectrometer, intense Rayleigh scattered light is filtered out using a Semrock E-Grade long pass filter (part number LP03-532RE-25). The filtered light is focused through a 50 μm slit for high spectral resolution and diffracted through a dual-region volumetric phase holographic transmission grating manufactured by Kaiser Optical Systems Incorporated. The two diffraction regions on the grating allow for low and high frequency Raman shift detection in a single exposure and cover a wavelength range of approximately 530-700 nm, or 73-4500 cm⁻¹ of Raman shift from an incident wavelength of 532 nm. The shortest detectable Raman shift with this setup is approximately 80 cm⁻¹ due to the filter’s pass band rising edge width.
2.3 Camera and Gate Timing

A Princeton Instruments PIMAX-I ICCD camera was used to detect the Raman scattered light collected by the system. The camera is mounted directly to the spectrometer housing at its output focusing lens. A variable gain intensifier is integrated into the camera housing and allows for amplification of the inherently weak Raman signal. Signal to noise ratio was farther improved by running the camera in intensifier gated mode, which reduces background signal collected in an exposure by only powering the intensifier when Raman scattered light is detectable. Optimal gate width and delay were found experimentally for each sample.

ICCD cameras are one solution available to overcome signal to noise limitations which are found in unamplified signal collection methods by offering both amplification of collected signal and gated operation, which reduces background signal in an exposure. Raman data from the mixed sample and the 5 pure sample dataset were collected with the camera operating in gated mode. Gated operation
of the camera is achieved by precisely controlling when power is supplied to the intensifier tube’s microchannel plate.

Figure 6 shows the timing used for gated operation of the ICCD camera. The main trigger utilized for gated mode was the laser’s “Q-switch sync” signal which consistently pulses 70nS before light exits the aperture. The camera waits after the main trigger to allow the laser pulse to travel to the sample and scatter back to the photocathode of the intensifier tube (gate delay). The intensifier gate is then opened allowing intensified light into the camera (Raman detectable). Ideal gate width can vary for each sample and was found experimentally for all data collection.

2.4 System Performance

As shown, the assembled system was able to collect Raman spectra and fluorescence signals from a wide variety of samples. Figures 7, 8, and 9 show calibrated ruby fluorescence, Raman spectra of room temperature water, and Raman spectra from various mineral samples respectively. All the data below was collected with no backstop at 20 cm from the receiver. All Raman data was collected with the system running in gated mode, the ruby fluorescence was collected with the camera running with a continuously opened shutter (CW mode). This system performed very well with mineral samples and was able to achieve good signal to noise ratio with clear liquid samples as well. Data collection of biogenic samples was attempted; however, the powerful visible spectrum laser caused high amounts of fluorescence and damaged some samples as well.
Figure. 7. Fluorescence spectra of Ruby crystal. Characteristic peaks at 693 and 694 nanometers can be seen along with a dim broadband signal ranging from 660 to 680 nanometers.

Figure. 8. Raman spectra of room temperature distilled water. The broadband signal ranging from 2900 to 3650 cm$^{-1}$ matches closely with other published data. Data point was collected with no backstop.
Figure 9. Raman spectra from calcite (A), quartz (B), and gypsum (C). Good signal to noise ratio was achieved using gated mode operation.
Experiments with the 532nm gated system described in Chapter 2 showed exceptional performance with mineral samples. Attempts to collect data from biological samples such as glutamine, however, showed heavy presence of laser induced fluorescence similar to that shown in Figure. 10. Due to the high energy per pulse of the UltraCFR laser, Raman spectra of biological samples consistently had intense fluorescent baseline. This chapter describes the design of a 785nm Raman spectrometer that will be used to reduce laser induced fluorescence in biological samples.

Figure. 10. Laser induced fluorescence overpowering 936(cm⁻¹) peak in naphthalene signal,
3.1 Laser excitation source

A Crystalaser QL785 Q-switched laser centered at 785nm was used as the laser excitation source for this Raman spectrometer. The compact size of the laser unit allows it to be mounted directly on top of the spectrometer enclosure. The laser is internally clocked to pulse at a rate of 1kHz with a pulse width of 10 to 15ns depending on power output setting. The laser is able to be externally triggered and also has an output signal in sync with its laser pulses, allowing for flexible usage in gated mode. Transmitter/receiver optics are shown below in Figure 11.

![Diagram](image)

Figure 11. Exterior lens setup for compact 785nm Raman spectrometer (side view). L1 = 18mm planoconcave. L2 = 150mm biconvex. L3 = 100mm planocylindrical. L4 = 50mm biconvex. M1 = mirror. F1 = dichroic beam splitter. S1 = 100um slit. The laser is mounted to the top of the spectrometer housing. Housing design based on that of SUCR instrument developed by Dr. Nurul Abedin.

3.2 Receiver and spectrometer

Laser light is directed to the sample in co-axial geometry by a mirror and a Semrock LPD02-785RU-25 long pass dichroic beam splitter with a pass band beginning at 792.9nm. Upon leaving the aperture, the laser light is directed through a 18mm planoconcave lens and a 150mm biconvex lens, to
increase the beam diameter to approximately 3.3mm. The expanded laser light is then focused onto the sample 10cm away with a 100mm planocylindrical lens. Backscattered light is then collimated by the cylindrical lens and focused onto the 50μm slit by the 150mm and 50mm biconvex lenses.

Inside the spectrometer (Figure. 12), light is collimated onto a Wasatch Photonics variable phase holographic grating by a Pentax c-mount camera lens and focused into the ICCD camera by a 2” diameter 50mm biconvex lens. The current grating has efficient diffraction to a Raman shift of 1600cm\(^{-1}\) from the incident wavelength of 785nm. The system has a supplemental Semrock NF03-785E-25 notch filter inside the housing to increase optical density past OD6 at the laser line.

3.3 Camera and Gating Scheme

A Princeton Instruments PIMAX-I ICCD camera was used to detect the Raman scattered light collected by the system. The camera is mounted directly to the spectrometer housing at its output focusing lens. A variable gain intensifier is integrated into the camera housing and allows for
amplification of the inherently weak Raman signal. Gated operation was attempted, however, both the camera and laser drivers are unable to trigger each other due to their trig-out signals having too short of a pulse width. In order for gated operation to be achieved, a separate external triggering circuit with a longer pulse width is needed. Intensifier delay and gate width can be set via software.

3.4 System Performance

Figure. 13 shows baseline noise that was always detected while the laser was running. Calibration of the noise verified that it was centered around the laser wavelength and that the center “trough” of the waveform was the notch filter’s stopband. Further data collection showed that the noise quickly degrades to similar intensities as Raman scattering. This is highlighted in Figure. 14 that shows the 473 cm⁻¹ peak of sulfur is detectable through the noise. The noise was present with two different 785 nm lasers, the Q switched laser described in Section 3.1 as well as a CrystaLaser DL-785 laser. Research into this issue pointed to either interference coming from the filters or amplified stimulated emission (ASE) noise being introduced by the pump diodes.

![Figure. 13. Baseline detected whenever laser backscatter is collected.](image-url)
A baseline correction program that was developed for data preparation for automated analysis proved to be useful in recovering signal that was on top of this noise. Figure 15 shows calibrated naphthalene spectra before and after baseline correction. The 513 cm\(^{-1}\) peak was able to be recovered from the baseline, functionality of this program will be covered in Chapter 5.

![Figure 15. Naphthalene signal before and after baseline subtraction. The 513 cm\(^{-1}\) peak was recovered from the baseline. Artifacts from the subtraction process are seen below 350 cm\(^{-1}\).](image)

![Figure 14. Sulfur signal visible through baseline. The baseline noise is on a similar intensity scale as Raman scattering.](image)
CHAPTER 4
MODEL ARCHITECTURE

The model presented in this thesis was able to detect multiple materials’ Raman signatures in a single line profile by splitting the task of detecting each individual signal to a single FNN. This model structure is similar to that of a matched filter, where each class has its own “known signal” that inputs are compared to. Replacing the class filters with an FNN grants the added benefit of lower probabilities of false alarm and higher probabilities of detection when there are multiple signals present in an input.

In this chapter, the architecture of the model will be explained. Additionally, the operating principals of the sub-FNNs, training and testing algorithms, and the procedure used for interpretation of the model’s output will be presented.

4.1 Feedforward neural networks

The model presented in this thesis makes use of multiple feedforward neural networks (FNNs) to detect multiple pure samples in a single input, one for each material it is trained to detect. FNNs were chosen for use because they lack the spatial encoding problems prevalent in convolutional neural networks (CNNs) while being easily scalable and fully adaptive. Improvements in performance over a traditional matched filter model were expected due to the learned aspect of each sub- FNN. By minimizing classification error with a pure sample training dataset, each sub-FNN will be attuned to the spectral features of its material and indifferent to all others in the training dataset. Each sub-FNN generated during training will follow the generalized structure shown in Figure. The input layer of the network is of the same length as the total length of all regions of the Raman line profile where spectral features of an arbitrary material are found. In its current iteration, the model uses an equal
number of hidden units for every sub-FNN. All sub-FNNs have a single output neuron, which acts as a single element of the overall model’s output.

The output of a single sub-FNN is calculated by applying weights, biases, and activation functions as normal. For an arbitrary input vector $x$, values at the hidden layer ($h$) are calculated using

$$h = \tanh((x \cdot \omega_h) + b_h) \quad (4.1)$$

where $\omega_h$ represents the hidden unit’s learned weights and $b_h$ represents the biases at the hidden units. Hyperbolic tangent was used as the hidden layer activation function. The selection of activation functions will be explained in section 4.1.2.

Output values are then calculated by

$$O = \sigma((h \cdot \omega_o) + b_o) \quad (4.2)$$
where $\omega_o$ represents the output neuron’s learned weights and $b_o$ represents the output’s bias. Sigmoid (Equation 4.3) was used as the output neuron’s transfer function.

$$sigmoid(n) = \sigma(n) = \frac{1}{1 + e^{-n}}$$

(4.3)

### 4.1.1 Activation Functions

The choice of activation functions in an FNN is critical in their design as it directly impacts the difficulty of training, the ability to converge during training, and the network’s highest potential accuracy. In an FNN, the activation functions of the hidden and output layers perform mathematical operations on the data that is being fed to them. In some cases, such as a classical perceptron, this can be a simple step function that only activates if the input is greater than a set value. More commonly, however, non-linear functions such as sigmoid (Eq. 4.3) and hyperbolic tangent are used because they allow the FNN to approximate more complex functions.

The model presented in this thesis makes use of hyperbolic tangent as the hidden layer transfer function and sigmoid as the output layer activation function for all sub-FNNs. These were chosen because of the format the input data as well as the desired meaning of the output. Utilizing hyperbolic tangent in the hidden layer centers all data passed forward to the output layer around zero (normalizes the data), this capability is what allows this architecture to function without a normalization step in preprocessing. The use of sigmoid on the output layer scales the data to the range of zero to one inclusively, allowing the activation of each sub-FNN to be thought of as a probability that its component material is present in the model’s input.

### 4.1.2 Training Methods

The “training” of an FNN involves the minimization of the network’s error by iteratively changing the weights between neurons. Very commonly, FNNs are trained utilizing “error
backpropagation,” which adjusts each weight by calculating its contribution to the error of the FNN as a whole.\textsuperscript{15} Let the output of the FNN in Figure. 16 be defined as:

\[
O = \sigma((\tanh(x \cdot \omega_i) + b_i) \cdot \omega_o) + b_o)
\]  

(4.4)

Where \(x\) is the input to the FNN, \(\omega_i\) and \(\omega_o\) are the learned weights for the input and output layers respectfully, and \(b_i\) and \(b_o\) are the biases for the input and output layers respectfully. When using mean squared error as the training loss function, the FNN’s error can be calculated with:

\[
E = \frac{1}{N} \sum_{i=1}^{N} (t_i - O_i)^2
\]

(4.5)

where \(N\) is the number of neurons in the output layer and \(t\) is the known value (target) that the output should be for a given input. Error backpropagation calculates the partial derivatives of \(E\) with respect for every weight in the FNN.\textsuperscript{15} The weights are then updated by Eq. 4.6, for all \(i\) weights in the network:

\[
\omega_i^+ = \omega_i^- - \lambda \frac{\partial E}{\partial \omega_i^-}
\]

(4.6)

where lambda is a decimal value called the learning rate. The learning rate is gradually reduced throughout training as a function of error to prevent the divergence from a local error minimum.\textsuperscript{13}

All sub-FNNs generated in this model were trained using Levenberg-Marquardt backpropagation (LMB). LMB is one of several algorithms which may be used to minimize cost function of, or train, a feedforward neural network.\textsuperscript{24} LMB was developed to solve inefficiencies found in error backpropagation. Despite traditional backpropagation’s still widespread use it is understood to be inefficient due to the need for small step sizes and the possibility of non-uniform curvature of the error function’s surface causing slow convergence.\textsuperscript{34}

A sub-FNN’s cost as a function of an arbitrary weight is likely to have several local minima given this problem’s dimensionality. Having too large of a learning rate can cause the training to
diverge from an ideal minimum and having too small of a learning rate can add unnecessary time to training. LMB solves these issues for small to medium sized problems by incorporating the Gauss-Newton algorithm when error function curvature is low, approximating the cost function as a quadratic equation for much faster computation. Although LMB is slower than a pure implementation of Gauss-Newton, it is faster than vanilla backpropagation and can be implemented on larger networks than Gauss-Newton alone.

Additionally, in this implementation the exit status of the shallow neural network training tool was monitored during model generation. A sub-FNN was only accepted if the training tool exited upon reaching the default minimum gradient value. During the model’s development, decreases in testing accuracy were noticed if sub-FNNs that exited training on a validation stop were used. If a validation stop was detected by the main model generation program, a new sub-FNN was trained until a minimum gradient stop was achieved.

4.2 Model generation procedure

The generation process for the model presented in this thesis can be seen in Procedure 1.10,17

<table>
<thead>
<tr>
<th>Procedure 1 – Model Generation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. <strong>for</strong> each pure sample $i$ in training data</td>
</tr>
<tr>
<td>2. detect regions of line profile containing spectral data</td>
</tr>
<tr>
<td>3. initialize fnn with input length equal to the sum of all region lengths</td>
</tr>
<tr>
<td>4. create a two class training dataset by extracting regional data</td>
</tr>
<tr>
<td>5. train fnn using two class dataset</td>
</tr>
<tr>
<td>6. <strong>end</strong></td>
</tr>
</tbody>
</table>

The user passes a labeled dataset of pure sample Raman spectra to the model along with the number of hidden units they would like in each sub-FNN. In this implementation, training observations and labels are passed as two separate matrices to the training script.
Model generation is completed by iteratively training each sub-FNN, the procedure for each sub-FNN is the same. To assist with network differentiation between pure samples and to ease computational burden, each sub-FNN limits where it searches an input line profile to only areas where spectral features of the material it is meant to detect are found on the Raman line profile, referred to as “regions of interest.” After these regions are defined for a single sample type, the model generates training data subsets for sub-FNN training. These subsets consist of the initially passed training data which has been trimmed to only contain features from the regions found in Procedure 1 Step 2 and the labels of this modified dataset are changed to only be two classes. The first class is for the material assigned to the detector network being trained and the second is for spectral data from all other classes. The modified datasets are then used to train the sub-FNN.

4.3 Model analysis procedure

The analysis process for the model presented in this thesis can be seen in Procedure 2.

**Procedure 2 – Analysis Algorithm**

1. for each sub-FNN \( i \) in a trained model
2. extract spectral data from the sub-FNN’s line profile regions
3. forward propagate extracted data through the sub-FNN
4. if threshold activation reached
5. report pure sample as detected
6. else
7. report pure sample as not detected
8. end
9. end

Classification of an input data point is accomplished by iteratively analyzing an input line profile with each trained sub-FNN. Line profile data from each sub-FNN’s regions of interest is extracted from the input. The extracted data is then forward propagated through the sub-FNN. The output values of each sub-FNN are then concatenated into a one-dimensional matrix and returned to the
user. If a user-set threshold activation is met on a class’ output, spectral features from that class are then considered present in the input.

4.4 Interpreting the model’s output

After a model is trained, it can be thought of as a collection of functions \( F \) that map certain sections of an input line profile \( x \) to a single member of an output row matrix of activation values \( Y \), as shown in Equation 4.7.

\[
Y = F(x)
\]

\[
y_i = f_i([x_{i1}, x_{i2}, ..., x_{in}])
\]

When transformed to an element-wise form (Eq. 4.8) \( y_i \) represents a specific member of the output row matrix, \( f_i \) represents the function acting upon an input when forward propagated through its respective sub-FNN, and \( x_{ij} \) represents the \( j^{th} \) region of interest from the \( i^{th} \) sub-FNN. All spectral data from the regions of interest is concatenated into a single vector before being passed to a sub-FNN.

It is up to the user of the model to decide at what activation a material can be labeled as detected/present, this point will be referred to as the activation of significance (AOS). The following method was used to find the AOS for analysis of the real mixed sample data collected in this thesis. After training, pure sample data (not from the training dataset) was classified using the model. For each class the max, mean, and standard deviation of activations from all non-member observations were calculated. The AOS was then set to the highest value of all max activations and all mean activations plus 3 standard deviations, following Eq. 4.9, for all \( i \) classes in the model. While it is possible to have a different AOS for each class, it is not recommended as it may increase the probability of a false alarm.

\[
AOS = argmax\{\max(y_i), \mu_i + 3\sigma_i\}
\]
CHAPTER 5
MODEL VALIDATION

The capabilities of the presented model were validated by analyzing real mixed sample Raman data and simulated mixed sample signals. One real mixed sample experiment and two simulated experiments were conducted. The real mixed sample experiment analyzed a sample with two components. The two simulated mixed signal experiments made use of Raman spectra datasets of 5 and 23 samples. Spectral data from the 5-class dataset was collected all on the same system by hand in NASA LaRC’s Raman spectroscopy lab, directed by Dr. Nurul Abedin. Spectral data from the 23-class dataset was acquired from the RRUFF project’s public “excellent oriented” and “excellent unoriented” datasets.14

5.1 Data Preparation

Although collecting Raman spectra in gated mode greatly reduces the amount of fluorescent background that is present in a line profile, baseline signal correction was performed on all data to ensure consistency in the training data set allowing only the network’s ability to recognize Raman features to be tested. In this thesis, baseline correction was accomplished by asymmetric least squares smoothing following the method presented by Eilers and Boelens in their 2005 release.35

All steps beginning from line profile extraction to a baseline corrected line profile combining high and low frequency regions can be seen in Figure. 17. Raw line profiles are extracted from the high and low frequency regions on the CCD (A – D). Baselines are then estimated and subtracted from the line profiles (E - F). The corrected line profiles are then concatenated, completing a single data point (G). This process was repeated for every training and testing data point, except when no features were
present in either the high or low frequency region. If no spectral features were present, the base signal was extended to fill in the missing region for consistent input length.

Figure 17. Steps in data preprocessing process. Line profiles (C & D) are extracted from raw CCD images (A & B) by vertically summing columns of pixels. The baseline of the extracted signal is estimated and subtracted (E & F) and the two regions are concatenated.
5.1.1 Smoothing with Asymmetric Least Squares

Broadband fluorescence found in Raman data was corrected by subtracting an estimated baseline signal from the low and high frequency regions before concatenation. The baseline signal was estimated using the same method developed in Eilers and Boelens 2005 release. This method generates a slowly varying baseline estimate using a Whittaker smoother with the caveat that positive deviations from the baseline estimate are punished far more than negative ones, adding the asymmetrical aspect.

The asymmetric Whittaker smoother operates by estimating a baseline series $Z$ with equal length $N$ to an input line profile $X$. The baseline series is meant to have the properties of being faithful to $X$ while still being smooth. These two properties can be combined in a cost function $C$, shown below in Equation 5.1, where $\Delta^2 Z_i = Z_i - 2Z_{i-1} + Z_{i-2}$. The first term of $C$ corresponds to the “faithfulness” property, where the estimated baseline $Z$ has as little difference from the input $X$ as possible.

$$C = \sum_{i=1}^{N} \omega_i (X_i - Z_i)^2 + \lambda \sum_{i=1}^{N} (\Delta^2 Z_i)^2 \quad (5.1)$$

The second term acts to penalize deviations in the estimated baseline by increasing cost when the baseline follows spectral features in the input. The term “$\lambda$” is a user-set parameter meant to balance the two terms and can be thought of as controlling the desired smoothness of the estimated baseline. “$\omega$” is a generalization weight vector which allows for recalculation of $Z$ by iterative updating.

Minimizing this cost function leads to the Equation 5.2:

$$(W + \lambda D'D)Z = WX \quad (5.2)$$

Where $W$ is a sparse diagonal matrix of $\omega$ and $D$ is a difference matrix “$DZ = \Delta^2 Z$.” Code implementation can be split into two calculations. With a known approximate solution, $Z'$, a new
weight vector, $\omega^*$, can be calculated by asymmetrically updating the weights with a new parameter $p$. An individual weight, $\omega_i$, will equal $p$ if $X_i > Z_i$ and equal $1 - p$ otherwise. The new weight vector is used to calculate a new approximate solution, the process is then repeated for a user-set amount of iterations or until little change in the weight vector is found. MATLAB implementation of this scheme is simple and fast, typically needing less than 10 iterations to converge, and was of great use for data preprocessing. The two user-set parameters, $p$ and $\lambda$, were found by trial and error for the mixed sample dataset and the 5-class pure sample dataset which were collected at NASA. No baseline correction was necessary on the datasets maintained by the RRUFF project.

5.2 Mixed sample analysis

The mixed sample that was analyzed was a two-component mixture of naphthalene and sulfur. This mixture of materials was selected for the sample because both components have bright spectra with minimal baseline when data is collected with the system running in gated mode. The total material in the sample weighs 7 g with 2.5 g of coarsely ground naphthalene and 4.5 g of finely ground sulfur (7.194 mol sulfur : 1 mol naphthalene). The overall sample area was restricted by wrapping the sample bottle in white paper with a 1 cm by 1 cm square hole cut in it. After sufficiently mixing the sample, it was placed on a 2-axis kinematic micrometer stage oriented for control over the Y and Z axes. The bottle was not directly moved from its initial placement on the stage to ensure the sample inside the bottle did not shift during data collection. The diameter of the laser beam was approximately 1mm at the strike point. A picture of the uncovered sample bottle can be seen in Figure. 18. A high contrast image of the 1 cm$^2$ sample window can be seen in Figure. 19.
Figure. 18. Image of mixed sample.

Figure. 19. High contrast image of analyzed area.
The model used to analyze this sample was trained with the 5-class dataset collected in NASA LaRC’s Raman lab. The data points from this mixed sample were collected on the same 532 nm Raman system described in Chapter 2. Despite the mixed sample only containing 2 of the 5-classes which are in the dataset, the model was trained for all 5-classes to see if any false positives would be reported. As shown in Figure. 20, the training time was rather quick, requiring just under 6 seconds for all 5 sub-FNNs to be prepared. All 5 of the sub-FNNs exited training upon reaching Matlab’s default minimum gradient and required no retries due to a validation stop. Default values were used for the minimum gradient, minimum error, and validation check training hyperparameters.

Figure. 20. Console output for training of 5-class model. The commands display the system date & time (Y, M, D, H, M, S) at the beginning and end of model training as well as the sub-FFN training exit states.

Figure. 21. Average naphthalene signal from training dataset with marked region of interest boundaries. The vertical lines show which regions of the line profile were found by the model to contain spectral features.
Figures 21 and 22 show the average naphthalene and sulfur signals across the training dataset. The vertical line surrounding individual peaks or groups of peaks are the boundaries of the regions of interest found by the training program. The program found 8 regions of interest for classifying naphthalene and 2 for classifying sulfur. Table 1 shows the mean, standard deviations, mean plus 3 standard deviations, and max activation values expressed by each sub-FNN when presented with a non-member input. AOS for this experiment was set to be the largest of all these calculated values, 0.1203.

<table>
<thead>
<tr>
<th>Class</th>
<th>Alabaster</th>
<th>Ice</th>
<th>Water</th>
<th>Naphthalene</th>
<th>Sulfur</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu$</td>
<td>2.16E-06</td>
<td>5.29E-06</td>
<td>1.18E-06</td>
<td>9.27E-06</td>
<td>6.90E-04</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>1.67E-05</td>
<td>7.56E-05</td>
<td>1.32E-05</td>
<td>8.92E-06</td>
<td>9.10E-03</td>
</tr>
<tr>
<td>$\mu+3\sigma$</td>
<td>5.21E-05</td>
<td>2.32E-04</td>
<td>4.08E-05</td>
<td>3.60E-05</td>
<td>2.80E-02</td>
</tr>
<tr>
<td>max</td>
<td>2.87E-04</td>
<td>1.40E-03</td>
<td>1.65E-04</td>
<td>1.65E-04</td>
<td>1.20E-01</td>
</tr>
</tbody>
</table>

Table 1: Mean, standard deviation, 3 sigma, and max activation values for all non-member observations of all sub-FNNs. Max value, used as AOS, is highlighted.
Figure 23 shows the front image of the mixed sample with a superimposed grid of color-coded spots. Each spot on the image overlay represents the center of the laser strike-point for a single data point. Between each exposure, the sample was carefully moved in steps of 1 mm to ensure the mixture was not disturbed, data points were collected from a total area of 1 cm$^2$. The color of each spot corresponds to the label(s) that the model applied to that data point. A red spot means features from both naphthalene and sulfur had activations above the AOS, a yellow spot means only sulfur features had activation above the AOS, and a green spot means only naphthalene features had activations above the AOS.

Figure 23. High contrast image of mixed naphthalene and sulfur. Red = mixed classification, yellow = sulfur classification, green = naphthalene classification. A series of naphthalene and mixed classifications can be seen to follow the while vein of naphthalene present from (1,1) to (9,8).
A series of mixed and naphthalene classifications can be seen to follow the white vein of naphthalene as it extends diagonally upwards from data points (1,1) to (9,8). Due to how fine the sulfur was ground a small amount of sulfur powder was covering all of the larger chunks of naphthalene, which is not clearly visible in the high contrast sample image. The darker areas of the image correspond with voids in the sample itself, where less material was pressed directly against the sample bottle. No false alarms were reported for any of the non-present classes (alabaster, ice, and water).

5.3 Simulated mixed sample signals

Two simulations were conducted to test the model’s accuracy when passed inputs containing spectral features of more than two samples and to verify pure sample classification accuracy matches accuracies achieved by current models. In both simulations, completely random combinations of a set amount of total classes were generated by adding average class signals together following Equation 5.3 where $x_s$ is the combined signal, $a$ is a random value between [0.1, 1.0] rounded to the nearest tenth, and $x_i$ is the average signal of a randomly selected sample class with intensity values scaled between 0 and 1.\textsuperscript{12,13} The total amount of class averages added together, $N$, is set by the user. Special care was taken during coding to ensure no one class could be selected twice.

$$x_s = \sum_{i=1}^{N} a x_i$$  \hspace{1cm} (5.3)

Two datasets were used to generate two different models. The first dataset consists of Raman data from 5 different samples collected all on the same system in the Raman lab. The second dataset consists of Raman data from 23 different materials and was generated by picking samples out of two combined Raman databases which had at least 50 unique observations. Because the databases maintained by the RRUFF project contain many data points taken on different systems, all Raman line profiles were scaled to a single x-axis with a set $dx$ of 0.5 (cm$^{-1}$). The 23-class dataset was left balanced (equal amount of training observations per class) to counteract the expected negative effect that x-axis
scaling would have on classification accuracy. The scaling process will be discussed in depth in Section 5.3.3.

Performance of the model in these experiments is quantified by calculating the probability of detection ($p_d$) and probability of false alarm ($p_{fa}$) for any arbitrary component signal in $x_i$. For both datasets: all sub-FNNs in the model had 200 hidden units, the AOS was set to a constant value of 0.5, 1000 iterations were run for every $N$, and $N$ was swept from 1 to the total amount of classes in the dataset. For all iterations where $N$ equaled 1, random noise was added along with the intensity scaling to increase differences between the simulated signal and the training data. Information pertinent to both model’s training processes will be provided in their respective sections. The results of each combined pure signal experiment will show the $p_d$ and $p_{fa}$ values for all values of $N$ and the prevalence of each pure sample in all observations where the model failed to detect at least one component signal. Comments will be made on any visible trends in the failed observations.

5.3.1 Traditional Matched Filter

The combined “excellent oriented” and “excellent unoriented” databases maintained by the RRUFF project contains Raman spectra from over 1600 minerals. For this experiment, mineral classes with at least 50 observations were selected and a balanced dataset was created from these data points. In total, this dataset contains 1150 unique data points from 23 total classes. The dataset was left balanced to help counteract the expected loss of accuracy from x-axis scaling. Data point scaling was accomplished by creating a new x axis ranging from 0 to 1577 cm$^{-1}$ with a constant $dx$ and extracting intensity values associated with the closest x value on the unscaled data point’s x axis. Any leading or trailing zeros were replaced with random noise to prevent zero variance errors from occurring during training, no other modifications were made to the data points from the RRUFF databases. The feature
selection functionality of the presented model was implemented in this matched filter implementation by the same methodology to allow for a more direct comparison between the two models performances.

Figure. 24. shows the probability of detection (P_d) and probability of false alarm (Pfa) of an arbitrary signal being detected as a function of the amount of total materials in the randomly combined input (N). As expected, P_d decreases with the number of total signals in an input. It can be seen that the probability of detection rapidly decays as the N increases. Also, the probability of false alarm is unacceptably high in the cases of N equaling 1 through 8, reaching far above 90% in the N equals 1 case. Although this model is capable of detecting multiple Raman signatures in a single input, the high probability of false alarm poses too much of a risk to use matched filters even as a pure signal classifier.

Figure. 24. P_d and Pfa values plotted for all values of N in mixed pure sample signals experiment using 23 class data set from RRUFF databases and the matched filter model\textsuperscript{10}. Pd decays faster than the presented model, and Pfa is far higher than that of the presented model for the N equals 1 through 7 cases.
5.3.2 5-Class dataset

The 5-material dataset consists of Raman spectra from alabaster, water, ice, naphthalene, and sulfur. All data points in this dataset were collected on the same Raman system in the LaRC Raman spectroscopy lab, and the training dataset for the naphthalene and sulfur mixed sample experiment was derived from this dataset. The entire dataset was used for training and the AOS was set at a constant value of 0.5.

Compared to the naphthalene and sulfur real mixed sample experiment, which used exactly half of this dataset for training, total training time increased by 28% to 8.376 seconds. All sub-FNNs exited their individual training by reaching minimum gradient. Total simulation time for all 1000 signals for all 5 Ns took about 26 minutes, timing profiler output can be seen in Figure 25.

The analysis of the 5000 simulated signals took a total of 1605s, excluding generation. This results in an average analysis time of 0.3s per signal. Generation of the simulated mixed signals accounted for less than 1% total execution time.

![Profile Summary](image)

Figure. 25. Timing profiler output from 5-class simulated mixed signals
Figure 26. Composition of observations with at least one undetected component for all N in 5 class simulation. Legend labels are associated with bars left to right.

Figure 27. Probability of detection ($p_d$) plotted versus N with a line of best fit projecting $p_d$ for higher N values.

<table>
<thead>
<tr>
<th>N</th>
<th>Probability of Detection ($p_d$)</th>
<th>Probability of False Alarm ($p_{fa}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>0.9930</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>0.9590</td>
<td>0</td>
</tr>
<tr>
<td>4</td>
<td>0.8548</td>
<td>0</td>
</tr>
<tr>
<td>5</td>
<td>0.7130</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 2: Probability of detection and probability of false alarm ($p_d$ and $p_{fa}$) for all Ns in 5-class simulation.
Figure 26. shows what percentage of observations with at least one undetected component contained each pure sample signal for all values of N. For all 1000 iterations where N equaled 1, there were no misclassifications. In the cases where N equaled 2 and 3, it can be seen that observations containing both water and ice component signals were more likely to be misclassified. This is likely due to the similarities between water and ice Raman signatures. It can also be seen that as N increases the composition of misclassified signals begins to even out, this is indicative of the complexity of the signal becoming the limitation in $p_d$ instead of similarities between component signals. Because all generated signals contained all pure signals when N equaled 5, the complexity of the generated signal was the only possible cause of a failed classification.

Figure 27. shows $p_d$ plotted versus N along with a calculated line of best fit. The trend in this 5-iteration case shows $p_d$ decaying rather rapidly as N increases, however, as will be seen in the RRUFF 23 dataset results section, non-zero $p_d$ has been recorded with as high as 23 component signals.

**5.3.3 Preparation of spectra from RRUFF datasets**

Due to the Raman data in the RRUFF project’s datasets being collected on different systems, x-axis scaling needed to be performed for compatibility with the presented model. Figure 28. highlights the issues which needed to be solved before use. Subplots A and B show two different calcite Raman spectra data points from the RRUFF project’s “excellent oriented” database before scaling. The 155, 281, 711, 1085, and 1434 cm$^{-1}$ Raman peaks can be seen in both. Neither system was able to detect the 1748 cm$^{-1}$ Raman peak. This could be due to the sensors not being large enough to detect diffracted light of that wavelength or the spectrometers diffractive optic not functioning at that wavelength at all. Although both data points were calibrated well on their own systems, x-axis scaling needs to be performed to correct the mismatching input lengths, standardize the total range of Raman shift covered in the line profile, and correct unequal spectral resolutions.
Line profile scaling was performed by creating a new Raman shift \((x)\) axis for all data points to follow and assigning intensity \((y)\) values from the source line profile for each point on the new \(x\)-axis. The new Raman shift axis ranges from 0 to 1577 \(\text{cm}^{-1}\), based off of the longest shift detected in a data point, and has a constant \(dx\) of 0.5 \(\text{cm}^{-1}\) for a total input length of 3155 units. Any leading or trailing zeros left over in the scaled data point were replaced with random values between 0 and 1 to prevent zero variance cases from occurring during model generation. In cases where the source line profile had a higher spectral resolution than the new \(x\)-axis (a \(dx\) less than 0.5 \(\text{cm}^{-1}\)) some data was lost in the scaling process. This loss of data could lead to an increased probability of false alarm and a decreased probability of detection. Figure 29. A and B show the same calcite data points after they had been scaled to the same Raman shift axis. Peak positions are calibrated to the closest 0.5 \(\text{cm}^{-1}\) from their original positions and the overall length of the line profiles is now the same.
This 23-class simulation uses the same dataset that was used to test the traditional matched filter. Training of the 23-class model for this experiment took just over 2 minutes. All sub-FNNs exited training by reaching minimum gradient. Total simulation time for 1000 data points over 23 values of N took 11 hours and 9 minutes, a screenshot of the timing profiler can be found in Figure 30. Figure 31 shows $p_d$ and $p_{fa}$ plotted versus N along with a calculated line of best fit. The trend in this 23 iteration case shows $p_d$ decaying rather rapidly as N increases, however, the rate of decay in $p_d$ decreases as N increases, appearing to reach an asymptotic minimum at 14%. The $p_{fa}$ appears to have no rate of growth or decay with a max value of 0.037167 at N = 6. The false alarms could be caused by similarities between the Raman spectra of different classes and by the use of a scaled x-axis as the scaling process did lead to a loss of information in data points which had a smaller $dx$ than 0.5 (cm$^{-1}$).
Figure. 30. Matlab timing profiler output from 23 class simulated mixed signals. Entire run took 11 hours and 9 minutes averaging 1.7 s to analyze a single line profile.

<table>
<thead>
<tr>
<th>Function Name</th>
<th>Calls</th>
<th>Total Time</th>
<th>Self Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>i23</td>
<td>1</td>
<td>40147.035 s</td>
<td>0.342 s</td>
</tr>
<tr>
<td>random_comb_23class_200HJU_check</td>
<td>23</td>
<td>40146.587 s</td>
<td>203.619 s</td>
</tr>
<tr>
<td>patRecPAT</td>
<td>23000</td>
<td>39933.727 s</td>
<td>246.869 s</td>
</tr>
</tbody>
</table>

Figure. 31. pd and pfa values plotted for all values of N in mixed pure sample signals experiment using 23 class data set from RRUFF databases.
Figure 32. Composition of observations with at least one undetected component for all N in 23 class simulation. Top to bottom of legend labels follow bars left to right.
Figure 32. shows what percentage of observations with at least one undetected component contained each pure sample signal for all values of N. For all 1000 iterations where N equaled 1, there were no misclassifications. In the N = 2, 3, and 4 cases, it can be seen that some component signals are in significantly more misclassified observations than other. This is possibly due to the use of a scaled x-axis and the varying spectral resolutions which are seen in this dataset. It can also be seen that as N increases the composition of misclassified signals begins to become more consistent, however, some samples are still significantly more common in misclassifications than others. For example, when N = 21 Albite was about 7% more common in misclassifications than Titanite.
CHAPTER 6
DISCUSSION

This chapter summarizes the development of the Raman systems and the improved matched filter model. Results from model validation and future work which could increase spectrometer performance and model accuracy will be discussed.

In this thesis, an improved matched filter model for classification of Raman spectra and two Raman spectrometer systems were developed and tested. The 532nm gated system was designed to use a high-powered laser at a reasonable sample distance suitable for lab use. The system used an off-the-shelf camera and spectrometer housing. The spectrometer was equipped with a custom, two region VPH grating made by Kaiser Optical Systems for high diffraction efficiencies up to 4500 cm$^{-1}$ of Raman shift. The spectrometer was equipped with high optical density Semrock long pass filter allowing the system to detect shift as low as 80 cm$^{-1}$. The transmitting optics utilized a prism allowing the laser to be used at full power and coaxial geometry for optimal backscatter collection.

The receiving optics utilized a 2” diameter collection lens to collect more backscattered light and a 20x microscope objective was used to focus light into the spectrometer for optimal collimation in its filtering section. The ICCD camera was equipped with a gated intensifier, experiments were run in gated mode to optimize signal to noise ratio and to allow for more comfortable operational conditions with the room lights on. In the past, this laser and spectrometer have not been able to receive Raman signal at samples distances this short. The 532 nm system performed well with mineral and liquid samples, however, there was high levels of laser induced fluorescence when biological samples were used. Performance of this system could be improved by reducing the size of the telescope section of the
receiver and installing a dichroic that is capable of withstanding the high energy laser pulses, increasing the efficiency and amount of backscatter collected by the receiver.

The 785 nm Raman system was designed to incorporate a pulsed near infrared laser in an ultra-compact package. The spectrometer enclosure was made in-house following the designs for the SUCR instrument developed by Nurul Abedin. The enclosure serves as the main mounting point for all optical components including the laser, allowing for simple integration into remote controlled platforms. The transmission optics direct laser radiation for coaxial alignment and the cylindrical lens shapes the laser beam to a micrometer scale width. The lower laser energy allows for a dichroic to be used, increasing collected backscatter. The 785nm system utilized a laser that is able to be externally triggered, allowing for gated operation with the same camera form the 532nm system. Data collected with the 785 nm system showed baseline noise on a similar intensity level of Raman scattered light. Raman signals that were on top of the baseline were able to be recovered with a correction program developed in house. The baseline signal could be improved by incorporating a laser line cleanup filter, to remove any amplified spontaneous emission noise from the pump diode, or by experimenting with other filters in the case the signal was introduced by interference or etalon effects. Gated functionality could be added to the 785 nm system by incorporating a main trigger circuit with a longer pulse width that both the camera and laser drivers can detect.

The model’s framework consists of multiple feedforward neural networks which are used in parallel to detect the presence or lack of spectral features from every component it was trained with. Implementation in Matlab allows the model to be scalable to any number of pure samples as the user wishes. Lab data was collected from 5 different pure samples as well as a 2-component mixed sample for training and validation. Raman spectra from publicly accessible databases maintained by the RRUFF project was also used to validate the model by simulating mixed sample Raman spectra
containing spectral features from up to 23 different materials. The model, analysis, and simulation programs were written in Matlab R2018a.

A feature selection subroutine was built into the model’s training program which only passes pertinent data forward to each sub-FNN, decreasing computational load of running multiple FNNs in parallel and the chances of a false positive from noise or non-important spectral features which may be present in other areas of the line profile.

Analysis of an arbitrary input signal is accomplished by iteratively forward propagating sections of a line profile through each sub-FNN. The areas of the line profile that are analyzed correspond to the regions of interest of each sub-FNN that were found during training. The model’s output consists of a 1-dimensional matrix of activation values from each sub-FNN in the order that they were trained. A positive detection for an arbitrary class is labeled as such by comparing the class’ respective sub-FNN’s activation to a user-set minimum. In this thesis the minimum activation value was calculated using equation 4.9. Each simulated signal was only analyzed once for both the 5 and 23 class datasets.

Model validation was accomplished by analyzing real and simulated Raman signals which contained spectral features from multiple pure samples. The real mixed sample data was collected from a mixture of naphthalene and sulfur. The classifications assigned by the model agreed with analysis done by visual inspection of the Raman line profiles. No false alarms for known non-present materials were reported.

Simulated mixed sample line profiles were generated by randomly combining class Raman signals.\textsuperscript{12,13} Two different datasets were used, the first was collected on a time gated Raman spectrometer built at NASA LaRC, the second was a combination of two publicly accessible databases maintained by the RRUFF project. Analysis of the real mixed sample data as well as the simulated mixed sample data showed that this model can detect multiple materials in a single line profile.
The simulated mixed sample performance showed that the model is capable of pure sample classification and can have non-zero probability of detection for signals containing as many as 23 different components. The simulation results also show that this model is not adversely affected by max intensities of an input signal deviating from those of the training dataset. When a traditional matched filter was tested with scaled inputs, classification failures were more common. By effectively using FNNs as class filters, this model was able to learn the important relative intensities of spectral features while placing no observed importance on overall signal intensity.

The model was developed into a custom scan analysis program that was designed for direct compatibility with the SUCR instrument developed by Dr. Nurul Abedin. Figure 33. shows the finalized analysis program window. When the number of classes present in a simulated signal are low, large differences in the composition of the misclassified signals can be seen. For example, when N
equaled 2 in the 5-class simulation, 100% of all signals with at least one failed classification contained both water and ice signals. Similar discrepancies were seen in the 23-class simulation, however, none were as extreme as the N = 2 run of the 5 class simulation. In both simulations, the composition of misclassified signals becomes more consistent as N increases. Both the 5 class and 23 class simulations show the probability of detection dropping off quickly as the number of classes in a simulated signal increase. This is likely due to distinct spectral features being “hidden” by combinations of other spectral features. The 23-class simulation shows that the decay rate of $p_d$ slows as N continues to increase and never actually reaches zero.

Due to Raman spectra of mixed samples being a combination of the pure sample line profiles, probability of detection could be increased by changing the analysis procedure. Incorporating code that will subtract away spectral features of classes that reached the AOS and re-analyze the signal for any classes not found in the first run and repeating until no more materials are found could allow for classes with lower relative intensity to be detected as long as matrix effects are not a factor in the detected signal.

A change in model architecture entirely could also allow for higher probability of detection and eliminate the need for OVA decomposition and feature selection as seen in this thesis. The recently developed “capsule net” is able to outperform CNN in image classification tasks and is capable of multi-label classification. Capsule net also greatly outperforms CNN when classifying highly overlapping image features. Although capsule net’s focus is image processing, the capabilities of capsules make good performance likely on 1 dimensional data. Other multi-label capable models are also available for simple implementation using Matlab or Python and scikit-learn.
CHAPTER 7

CONCLUSIONS

This thesis presented an improved matched filter model for classification of Raman spectra and two Raman spectrometer systems. The two spectrometers were able to detect Raman scattered light and the model showed improved probabilities of detection for mixed sample signals and much reduced probabilities of false alarm.

The 532 nm system was able to controllably use a high energy pulsed laser at sample distances convenient for lab use. The gated functionality of the ICCD camera enabled the system to operate with in ambient room light and improved signal to noise ratio. High quality mineral and liquid sample Raman data was able to be collected. The 785 nm system is equipped with a lower energy laser, reducing the effect of laser induced fluorescence. The ultra-compact enclosure also enables the system to be easily incorporated into a mobile platform. Improvements to the 785nm system can be made by adding a longer pulsed timing circuit to serve as the main trigger and a laser cleanup filter.

The model was tested with data from publicly accessible databases as well as from the 532 nm system. Real and simulated mixed sample Raman data was analyzed using the presented model. Mixed sample classification was achievable on all datasets that were tested, and non-zero detection probabilities were seen on simulated signals with as many as 23 components.

Although the presented model is capable of detecting multiple samples a single line profile, the probability of an arbitrary component’s Raman signal being detected decreases as the amount of present signal components increases. This model is also prone to issues in classification of Raman signals which have large amounts of overlap between each other, such as water and ice. Future research
into model improvements and architecture changes can increase classification accuracy and decrease computational load of training and analysis.
REFERENCES


APPENDIX A

FEATURE SELECTION FOR MODEL TRAINING

A.1. Necessity of feature selection

It was found early on in this model’s development that utilizing the entire Raman line profile for training and using only a single feedforward neural network for classification were not going to be possible when training with pure sample data only. Due to the need for one vs all decomposition, there will be high computational load during training and analysis if the full line profile is used as the input for every FNN that is in a trained model. To make training and analysis faster, code that locates the spectral features of each class and limits the input of each sub-FNN to those areas of the line profile was incorporated into the training program.

A.2. Feature selection methodology

Feature selection was accomplished by calculating mean and standard deviation of the average class line profile twice, once with all intensity values included in the calculation and a second time ignoring spectral data which rises above the first calculated mean plus a user set amount of first standard deviations. The data used in this thesis was able to work well with only 1 standard deviation, however, the optimal amount to add will change from one system to another. The second recalculation of the mean and standard deviation was found to be necessary to include dimmer spectral details and retain compatibility with broader Raman features such as those of ice and water. This process is visualized in Figure A1, the Sulfur Raman signal is shown with the first and second calculations of the signal mean plus one standard deviation (red and green lines respectively). The moment a signal rises above \( \mu_2 + \sigma_2 \) the model traces the signal to the left and right until it falls below \( \mu_2 \) again, this range of values on the line profile is called a “region of interest” (ROI) and is one of the areas of the line profile a sub-FNN will
analyze. As can be seen, dimmer spectral features may be missed if the first mean and standard deviation are used to define the ROIs. Due to this nature of zone definition, it is possible for multiple spectral features to be in a single ROI. It is also possible for two ROIs to share a beginning and end point due to how the code was written, this was not found to cause any issues during model validation.

![Region definition by double calculation of signal mean and standard deviation. Regions 1-4 are defined by where the line profile rises above the second mean and standard deviation.](image)

Figure A1: Region definition by double calculation of signal mean and standard deviation. Regions 1-4 are defined by where the line profile rises above the second mean and standard deviation.

ROIs for signals with no broad features were also able to be found by analyzing the “first derivative” of the line profile. Figure A2 shows an Auger plot of a sulfur Raman line profile calculated by finite difference. The spectral peaks have been replaced with sharp peaks immediately followed by sharp troughs, corresponding to the positive and negative slopes on each side of a Raman peak. ROIs could also be found by monitoring deviations from zero, as the first derivative is likely to have a mean very close to zero. Issues were found, however, when this method was applied to materials with wide Raman peaks, such as ice and water. The broad features have “flat” areas around their center, making
the first derivative close enough to zero for the program to think the feature had ended, as seen in Figure A3.

Figure A2: First derivative of sulfur Raman line profile.

Figure A3: Raman line profile of water and its first derivative. The values holding close to zero would cause the program to think the spectral feature had ended.
APPENDIX B

CLASSIFYING RAMAN DATA WITH FEEDFORWARD NEURAL NETWORKS

B.1. Formatting data for training and analysis

Matlab implementation of this model made use of the built-in libraries and shallow neural network training tool for the training of each sub-FNN. With this being the case, the format by which Raman data is passed to either the training or analysis programs was designed to be consistent with Matlab functions from the neural network and deep learning toolboxes.

A single training or analysis data point consists of a 1-dimensional matrix of the intensity values from a Raman line profile. This implementation assumes that the x-axis is the same across all the data points it sees, whether its units are pixels or nanometers or Raman shift is unimportant.

The model training program needs two matrices to begin training. The first, which will be referred to as “X”, is the training dataset and contains all full-length Raman line profiles that will be used in model generation. X will have the dimensions of [O-by-F] where O is the number of observations (or individual data points) in the training dataset and F is the number of features (or pixels) that are in a single data point. One row of X represents a single line profile. The second matrix needed by the training program, referred to as “Y”, contains the class labels of the training observations. Y will have the dimensions of [O-by-C] where O is the number of observations (Y must have the same number of rows as X) and C is the class that an observation belongs to. Due to each training observation only belonging to one class, Y will be a sparse matrix. Each row of Y will have zeros for all columns except for the class that the observation belongs to which will have a 1.

A softmax layer cannot be used as the output layer’s activation function because the sub-FNN output is a single neuron. Sigmoid was used in this model instead. Matlab should automatically set the
output layer activation function to sigmoid (Matlab calls it “logsig”) when it sees that the FNN was initialized with only one output neuron.

B.2. How feedforward neural network outputs are calculated

![Feedforward neural network structure](image)

Figure B1: Feedforward neural network structure with an input length of 5, 3 hidden units, and 1 output neuron.

Figure B1 shows the structure of a 3-layer feedforward neural network. Each circle represents a neuron and each line between neurons represents a learned weight. Each neuron in the FNN has a transfer function and bias associated with it. All together the FNN structure represents a series of equations which will calculate a value at the network’s output.

When the FNN is initialized, all weights and biases are typically random values. By training the neural network, ideal weights can be found which minimizes the output’s overall error. Training is
accomplished by minimizing an error function via gradient descent with respect to every weight in the FNN, mean squared error was used as the error function for all sub-FNN training in this thesis.

Output values are calculated by forward propagating an input through the network. All values in the input layer are first passed to the hidden layer. Each hidden unit performs a dot product with the input values and its learned weights, adds its random bias, and applies its transfer function. If, for example, the hidden layer’s activation function was hyperbolic tangent. Each hidden unit “$i$” would calculate its value using

$$h_i = \tanh((x \cdot \omega_i) + b_i) \tag{B1}$$

The output layer would then calculate its value(s) following a similar process. For each neuron “$j$” in the output layer, the hidden unit values would be dotted with the output neuron’s learned weights, its bias would be added, and its transfer function would be applied. If, for example, the output layer’s transfer function was sigmoid, the output values would be calculated using

$$O_j = \sigma((h \cdot \omega_j) + b_j) \tag{B2}$$

Where

$$sigmoid(n) = \sigma(n) = \frac{1}{1 + e^{-n}} \tag{B3}$$
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