Impacts of Oil Spills on Altimeter Waveforms and Radar Backscatter Cross Section

Yongcun Cheng
Old Dominion University, y1cheng@odu.edu

Jean Tournadre

Xiaofeng Li

Qing Xu

Bertrand Chapron

Follow this and additional works at: https://digitalcommons.odu.edu/ccpo_pubs

Part of the Oceanography Commons

Repository Citation
Cheng, Yongcun; Tournadre, Jean; Li, Xiaofeng; Xu, Qing; and Chapron, Bertrand, "Impacts of Oil Spills on Altimeter Waveforms and Radar Backscatter Cross Section" (2017). CCPO Publications. 202.
https://digitalcommons.odu.edu/ccpo_pubs/202

Original Publication Citation

This Article is brought to you for free and open access by the Center for Coastal Physical Oceanography at ODU Digital Commons. It has been accepted for inclusion in CCPO Publications by an authorized administrator of ODU Digital Commons. For more information, please contact digitalcommons@odu.edu.
Impacts of oil spills on altimeter waveforms and radar backscatter cross section

Yongcun Cheng1, Jean Tournadre2, Xiaofeng Li3, Qing Xu4, and Bertrand Chapron2

1Center for Coastal Physical Oceanography, Old Dominion University, Norfolk, Virginia, USA; 2Laboratoire d’Océanographie Physique et Spatiale, IFREMER, CNRS, Université de Bretagne Occidentale, Plouzané, France; 3GST, NOAA/NESDIS/STAR, College Park, Maryland, USA; 4College of Oceanography, Hohai University, Nanjing, China

Abstract
Ocean surface films can damp short capillary-gravity waves, reduce the surface mean square slope, and induce “sigma0 blooms” in satellite altimeter data. No study has ascertained the effect of such film on altimeter measurements due to lack of film data. The availability of Environmental Response Management Application (ERMA) oil cover, daily oil spill extent, and thickness data acquired during the Deepwater Horizon (DWH) oil spill accident provides a unique opportunity to evaluate the impact of surface film on altimeter data. In this study, the Jason-1/2 passes nearest to the DWH platform are analyzed to understand the waveform distortion caused by the spill as well as the variation of σ0 as a function of oil thickness, wind speed, and radar band. Jason-1/2 Ku-band σ0 increased by 10 dB at low wind speed (<3 m s⁻¹) in the oil-covered area. The mean σ0 in Ku and C bands increased by 1.0–3.5 dB for thick oil and 0.9–2.9 dB for thin oil while the waveforms are strongly distorted. As the wind increases up to 6 m s⁻¹, the mean σ0 bloom and waveform distortion in both Ku and C bands weakened for both thick and thin oil. When wind exceeds 6 m s⁻¹, only does the σ0 in Ku band slightly increase by 0.2–0.5 dB for thick oil. The study shows that high-resolution altimeter data can certainly help better evaluate the thickness of oil spill, particularly at low wind speeds.

1. Introduction

Geophysical parameter estimates from altimeter can often be degraded by very high surface radar backscattering coefficient (hereafter denoted by backscatter, σ₀), which indicate that the altimeter waveform model used to infer the geophysical parameters [Brown, 1977] is no longer valid. Several studies conducted using different altimeter data (Topex, Jason-1, and Envisat) have shown that these events named “sigma0 blooms” affect almost 6% of the measurements over the ocean. The global descriptions of the σ₀ blooms events are most of the time but not always associated with low winds [Mitchum et al., 2004; Thibaut et al., 2007]. It has also been hypothesized that surface slicks could play a significant role in σ₀ blooms. Two studies [Garcia, 1999; Tournadre et al., 2006] using analytical models of altimeter waveforms have well reproduced some observed σ₀ blooms for Topex and Jason-1 altimeters. The results demonstrate significant inhomogeneity of the surface backscatter, such as the ones associated with surface slicks, can cause σ₀ bloom events. However, it has not been possible to ascertain the relationship between oil slick and bloom, furthermore, to quantify the effect of oil slick on altimeter measurements, attributed to lacking of reliable surface oil films, information collocated, and coincident with altimeter data.

The Deepwater Horizon (DWH) oil spill event occurred on 20 April 2010. The reviews of the DWH oil spill event can be found in the literature [Fingas and Brown, 2014; Liu et al., 2013; Leifer et al., 2012]. It was the largest accidental marine oil spill in the U.S. petroleum industry history. The leak was finally stopped on 15 July 2010. The time-varying oil flow rate was estimated between 53,000 and 63,000 barrels/d [McNutt et al., 2011; Kourafalou and Androulidakis, 2013] and the total oil leak was 4.4 × 10⁶ ± 20% barrels (about 700,000 m³) [Crone and Tolstoy, 2010]. An extensive set of in situ and satellite (Synthetic Aperture Radar (SAR) and radiometers) data have been collected, archived, and distributed. The SAR, Moderate Resolution Imaging Spectroradiometer (MODIS) observations of DWH oil spill have been well documented in the previous studies [e.g., Bulgarelli and Dajvidnia, 2012; Garcia-Pineda et al., 2013; Jones et al., 2011; Leifer et al., 2012; Li et al., 2013; Liu et al., 2011; Minchew et al., 2012; Migliaccio and Nunziata, 2014; Sun et al., 2016]. In particular, all the available SAR and visible images during the spill have been processed to produce daily oil spill...
extent and thickness fields from 25 April 2010 to 28 July 2010. This unique data set offers a new opportunity to evaluate and quantify the impact of surface film on altimeter data in three aspects. It helps us to first ascertain that surface film does cause σ₀ bloom, and then to analyze the wind condition under which bloom occurs, and finally to quantify the impact of film and its thickness on the measured σ₀.

Two altimeter passes close to the DWH platform are selected (Jason-1 pass 015 and Jason-2 pass 204, Figure 1). As the repeat period of both satellites is 10 days, 10 cycles of data can be analyzed during the 94 days when the DWH oil covered the ocean surface. Since both Jason-1 and Jason-2 altimeters operate at two frequencies: 13.5 GHz (Ku band) and 5.3 GHz (C band), it is also possible to investigate the frequency dependency of film’s impact. Envisat altimeter data are not considered in this study because of its longer repeat period of 35 days that limits the number of overpasses.

The paper is organized as follows. Section 2 presents the altimeter data description used in this study and in particular the surface backscatter field computed by inversion of the altimeter waveforms (see Appendix A). The DWH SAR and visible images, oil spill cover, and thickness data are also described in this section. Section 3 shows the analysis of three altimeter passes in presence of oil slick under different wind conditions. Section 4 analyzes all the altimeter data during the oil spill and estimate the mean impact of film as a function of wind speed, oil thickness, and sensor frequency. The results are discussed in section 5.

2. Data
2.1. Altimetry Data
An altimeter is a nadir looking radar that emits short electromagnetic pulses. It measures the backscattered power by the sea surface as a function of time to construct the echo waveform from which the geophysical parameters are estimated. A detailed description of the principles of altimetry is given for example in Chelton et al. [2001]. The backscatter coefficient of the waveform can be expressed as a double convolution product of the radar point target response, the flat sea surface response and the joint probability density function of slope and elevation of the sea surface [Brown, 1977]. Over an ocean surface, when we assume a Gaussian altimeter pulse, a Gaussian antenna pattern and a Gaussian random distribution of rough-surface specular points, the waveform has a characteristic shape that can be described analytically using the Brown model (see Figure 2).

The altimeter geophysical parameters: epoch (range), surface backscatter, and significant wave height (SWH) are estimated by fitting the theoretical Brown model to the measured waveforms using a maximum likelihood estimator (MLE) [Barrick and Lipa, 1985; Tournadre et al., 2011]. Two estimators, MLE-3 and MLE-4, are currently used in standard ocean operational processing. Both estimators compute three parameters (epoch, backscatter, and SWH), while the MLE-4 also solves an additional parameter of the off-nadir angle. The dual frequency signal is mainly used for the correction of ionospheric perturbations.

The Jason-1 and Jason-2 Sensor Geophysical Data Record (SGDR) data are available from the AVISO (Archiving, Validation and Interpretation of Satellite Oceanographic Data). The products provide along-track high-
rate (20 Hz) Ku-band waveforms as well as the geophysical and environmental parameters. The waveforms are given over 104 temporal bins of width equal to the altimeter pulse length. For Jason-1, \( \sigma_0 \) is estimated using the MLE-4 while the Jason-2 one is estimated using both MLE-3 and MLE-4. Along with the SGDR, \( \sigma_0 \) at a 290 m resolution over a 8 km wide swath computed by inversion of the waveforms [Tournadre et al., 2011] are also presented. The method is based on the fact that an altimeter can be seen as an imager of the sea surface backscatter whose imaging process is more complex than a classical one in the sense that pixels are not rectangular but annular. The imaging process of the sea surface, i.e., the transform matrix between the real and the waveform spaces, depends only on the satellite and altimeter geometry and can be analytically computed. The pseudo-inverse of the transform matrix can then be used to invert the waveforms in terms of surface backscatter. A more detailed description of the method is given in Appendix A.

2.2. Oil Spill Images and Oil Cover

The DWH oil spill has been well documented and several satellites (especially SAR missions) made daily acquisitions over the Gulf of Mexico during the event. The CSTARS (Center For Southeastern Tropical Advanced Remote Sensing), University of Miami, created the DWH Images database that contains all the SAR and visible images acquired during the oil spill (in general several a day), the NASA (National Aeronautics and Space Administration) Gulf Oil Spill Data, and airborne instrument database. Oil spill leaves a dark feature (e.g., low \( \sigma_0 \)) in SAR image [Buono et al., 2016; Cheng et al., 2011; Liu et al., 2010; Garcia-Pineda et al., 2013; Xu et al., 2015; Nunziata et al., 2015]. To confirm the altimeter waveform distortion related to the presence of oil spill, the collected SAR images (Envisat ASAR, Radarsat SAR [Zhang et al., 2011, 2017] and Cosmo-Skymed-1/3 SAR [Cheng et al., 2014]) from these databases have been collocated with the altimeter passes (e.g., within 1 day). The optical sensors such as MODIS show large contrast in sun-glitter imagery for oil spill. A MODIS-Terra image is used to compare with Jason-2 altimeter pass. During the spill, the Environmental Response Management Application (ERMA) was developed through a joint partnership between National Oceanic and Atmospheric Administration (NOAA) and the University of New Hampshire’s Coastal Response Research Center in order to maintain an archive of most of the data from the DWH Response and the Natural Resource Damage Assessment. Among this archive, we use the daily integrated oil cover produced by the U.S. Coast Guard, British Petroleum (BP), and NOAA. It utilized a combination of visual and remote sensing observations from aircraft, as well as satellites (SAR images from various satellites, Landsats Thematic Mapper (TM), NASA’s MODIS visible/near infrared (MVIS), and MODIS thermal (MTIR)), to detect the presence of oil in any thickness. The extent of oil on the surface is estimated for each image collected on a given calendar day, classifying the oil into categories based on specific spectral characteristics. The spectral information can be used to estimate an average oil thickness per category. The data are aggregated into the two semiquantitative categories of “thick oil” and “thin oil” to estimate oil coverage on a 5 km \( \times \) 5 km grid in the northern Gulf of Mexico and to calculate the percent coverage of thick oil and thin oil per grid cell per day. The data area is available on the ERMA website (https://gomex. erma.noaa.gov/) and the daily oil spill cover were systematically collocated with the altimeter passes.
3. Altimeter Data Analysis

Although SAR is a very powerful tool to operationally detect and monitor oil spill, it lacks of sensitivity to estimate the oil thickness. Its utility for monitoring oil spill trajectories is limited by the satellite revisit time and swath [Cheng et al., 2014] and the presence of many "look-alike" oil features in case of very low wind [e.g., Bao et al., 2016; Caruso et al., 2013; Kim et al., 2015; Li et al., 2009; Fiscella et al., 2000; Gade et al., 1998a, 1998b]. On the other hand, visible imagery such as MODIS suffers from cloud cover and is limited to day-time observation in sun glint region only [Hu et al., 2009; Xu et al., 2013; Zhao et al., 2014].

To illustrate the impact of oil spill on altimeter data and explore the capability of using altimeter data as a complement data set for oil spill monitoring, in particular for low wind condition, we present the analysis of the Jason-2 data along pass 204 from cycles 069 and 072 and Jason-1 data along pass 015 from cycle 306, which correspond to various meteorological situations.

3.1. Jason-2 Pass 204

3.1.1. Low Wind Case

The descending orbit Jason-2 pass 204 enters the Gulf of Mexico around 29.13\degree N (Figure 1). Figure 3a presents the 20 Hz waveforms along the Jason-2 pass 204 cycle 069 (25 May 2010 06:09 UTC). This case corresponds to a low wind situation for which the mean ECMWF (European Centre for Medium-Range Weather Forecasts) wind speed along the track was 2.9 m s\(^{-1}\). In Figure 3a, the x-label denotes the 104 samples (or range bins) of Jason-2 altimeter waveforms. The onboard tracker normally centers the waveform leading edge at a predefined central gate of 32.5 to keep the waveform well centered in the analysis window [e.g., Roesler et al., 2013]. Note that the obvious distortion of the waveforms near 28.25\degree N and 28.75\degree N perturbs the onboard tracker and results in the displacement of the leading edge. However, the waveforms leading edge epoch can be repositioned at the nominal central gate of 32.5 by a simple translation using the tracker position information given in the SGDR (Figure 3b) [Tournadre et al., 2006]. The C-band waveforms are presented in Figure 3c. They exhibit behaviors very similar to the Ku-band ones.

Figure 3d shows the along-track variations of Ku-band and C-band MLE-3 \(\sigma_0\) and mean inverted \(\sigma_0\). In Figure 3d, parabolic shapes are clearly visible in both Ku-band and C-band waveforms near 28.8\degree N and 28.4\degree N. The Ku-band MLE-3 \(\sigma_0\) reaches 20 dB. These shapes result from large variations of backscatter at small scale that distort the waveforms as shown by Tournadre et al. [2006]. In Figure 3b, the waveform measured at the center of the parabolic shapes (e.g., at 28.25\degree N) is different from the waveform measured at 28\degree N outside the parabolic shapes and follows very well the Brown model (Figure 2a). The waveform shape at 28.25\degree N is very similar to the one simulated using the Tournadre et al. [2006] model for a 5 km radius of 5 dB circular bright patch (Figure 2b).

Tournadre et al. [2009] demonstrated that the square of the off-nadir angle (hereafter denoted by off-nadir angle, \(\zeta\), related to the slope of the trailing edge of the waveform, is a very good indicator of the inhomogeneity of the surface backscatter within the altimeter footprint. Figure 4 presents the Ku-band \(\zeta\) estimated by the MLE-4 estimator and given in the SGDR. The \(\zeta\) estimated by the linear regression of Ku-band waveform trailing edge is also presented in the figure. Between 28\degree N and 29\degree N, \(\zeta\) anomalously oscillates and reaches very large values (positive and negative). The distortion is remarkable near 28.3\degree N and responsible for the MLE-4 estimator failure (data missing). The \(\zeta\) oscillations near 28.3\degree N and 28.6\degree N are typical of the presence of surface slicks and coincident to that described by Tournadre et al. [2006].

Figures 5a and 5b present the inverted surface Ku-band and C-band \(\sigma_0\) at 290 m resolution, respectively. In Figure 5b, the ERMA thin and thick oil cover are overlaid. Because of the altimeter sampling geometry, two symmetrical points with respect to the satellite track have identical images in the waveform space leading to a left/right ambiguity. The inverted \(\sigma_0\) is thus the mean of symmetrical points to the left and the right of the ground track. The inverted fields are plotted on both the left and the right of the satellite track. Figures 5c and 5d show the two collocated SAR images obtained with the closest time to altimeter measurements, e.g., Envisat (25 May 2010 15:47 UTC) and Cosmo-Skymed-3 (25 May 2010 11:57 UTC), respectively. The dark features (low \(\sigma_0\)) that denote the regions affected by oil spill appear very homogeneous with little backscatter variations. The figures clearly show that the presence of oil corresponds to increased surface \(\sigma_0\) in both Ku and C bands. Near 28\degree N, in thin oil, the \(\sigma_0\) increase is limited to about 0.5 dB, but it then grows to almost 10 dB near 28.3\degree N and 28.6\degree N where thick oil was detected by ERMA. Within the region of thick oil cover, the surface \(\sigma_0\) reveals the presence of two very bright patches: a linear one around 28.8\degree N and a roughly
They correspond to a very strong attenuation of the surface wave that is associated with thicker oil.

3.1.2. Moderate Wind Case

The second example, pass 204 cycle 073 (3 July 2010 21:45 UTC) concerns a case of moderate ECMWF wind of 8.7 m s\(^{-1}\). The repositioned along-track Ku-band and C-band waveforms, the off-nadir angle, and the Ku-band and C-band MLE-3 and inverted \(\sigma_0\) are presented in Figure 6. The MODIS Terra images (4 July 2010 16:40 UTC, Figure 7c) and Cosmo-Skymed-1 SAR image (3 July 2010 11:56 UTC, Figure 7d) as well as the oil cover ERMA analysis (Figure 7b) are presented in Figure 7. In Figure 7c, the oil spill is clearly visible within the sun glint region but cannot be distinguished from background outside. The SAR image (Figure 7d) captures well the extent of the oil spill but as in Figure 5 there is very little backscatter variability within the dark patch. In Figures 7a and 7b, it can be seen that the impact of oil on altimeter data is more limited than that at low wind (Figures 3 and 4). At C band, both waveforms and \(\sigma_0\) do not exhibit significant along track variation. At Ku band, a light parabolic shape can be detected near 28.75°N where the ERMA analysis shows circular one near 28.3°N. They correspond to a very strong attenuation of the surface wave that is associated with thicker oil.

**Figure 3.** (a) Measured Jason-2 Ku-band waveforms for pass 204 cycle 069. Repositioned (b) Ku-band and (c) C-band waveforms. The color scale represents linear backscattered waveform power. (d) Ku-band and C-band MLE-3 \(\sigma_0\) (red and black lines) and mean along-track inverted Ku-band and C-band backscatter (blue and green lines). Note that there is a typical difference (~2 dB) between \(\sigma_0\) values from Ku-bands and C-bands. The dashed green and red line represent the limits of the thin and thick oil cover within the altimeter swath.
the presence of thick oil (Figure 7b). It is associated with a local $\sigma_0$ increase of some tenth of dB (0.7 dB) and an oscillation of $\zeta$ (Figure 6c). The inverted $\sigma_0$ presented in Figure 7 shows that this parabolic feature corresponds to patch of enhanced surface backscatter of 1–2 dB. The inverted field also reveals another zone of locally enhanced (0.5 dB) backscatter near 28.6°N in the ERMA thin oil region. It could be associated with thick oil as shown in the Cosmo-Skymed-1 SAR image. Note that the local $\sigma_0$ increase within oil are of the same order of magnitude as some local maximums observed near 28.2°N, which are clearly related to wind variability.

Figure 4. Off-nadir angles for pass 204 cycle 069 from the MLE-4 estimator (solid line) and inferred from the waveforms plateau slope (dashed line).

Figure 5. Inverted high-resolution (a) Ku-band and (b) C-band $\sigma_0$ (in dB) for Jason-2 pass 204 cycle 069 (25 May 2010 06:09 UTC). The black and red dots in Figure 5b represent the ERMA thin and thick oil cover respectively. (c) Envisat ASAR image (25 May 2010 15:47 UTC). (d) Cosmo-Skymed-3 SAR image (25 May 2010 11:57 UTC).
3.2. Jason-1 Pass 015

The main difference between the two Jason altimeters is that the raw waveform data telemetered from Jason-1 used some, but not all, bin averaging in the trailing edge (bin 64–104) to reduce throughput, whereas all 104 waveform bins are transmitted for Jason-2 [Thibaut et al., 2004]. Unlike Jason-2, the noise level of the Jason-1 decompressed trailing edge data, which affects the noise on the inverted $r_0$. On the another hand, compared with Jason-2, only the MLE-4 geophysical parameters are available in the Jason-1 SGDR. Figures 8a–8d present the Jason-1 pass 015 (ascending orbit) cycle 310 (1 June 2010 18:45 UTC) reposited Ku-band and C-band waveforms, off-nadir angle and MLE-4 and inverted $r_0$. The pass corresponds to a very low wind speed (mean ECMWF wind of $1.9 \text{ m s}^{-1}$) situation and a large ERMA thick oil cover (Figure 9b) as shown on the Radarsat-1 and 2 images (Figures 9c and 9d) taken on the same day at 23:58 and 12:01 UTC, respectively. Compared with dark features in Figures 9c and 9d, Ku-band and C-band waveforms are obviously strongly distorted (Figures 8a and 8b) between 27.5°N and 29.5°N. Several parabolic shapes of different intensity can be seen at 27.75°N, 28.3°N, 28.6°N, 28.8°N, 29.2°N, and 29.5°N. Within these parabolic shapes, $\xi$ oscillates and sometimes exceeds 0.5 deg$^2$ leading to the failure of the MLE-4 estimator and data missing. The waveform distortion responsible to the MLE-4 Ku-band $r_0$ oscillates within the parabolic shapes due to the impact of $\xi$ on $r_0$ with the estimator.

The inverted high-resolution Ku-band and C-band $r_0$ and collocated Radarsat-1/2 images are shown in Figure 9. There is a very good overall agreement between the ERMA oil extent and the region of high inverted
Ku-band and C-band $\sigma_0$ (Figure 9b). However, compared to the SAR images and the ERMA analysis, the altimeter inverted $\sigma_0$ reveal the high variability at small scale of the surface backscatter within the oil-covered region. That is certainly associated with the thickness of oil, which is not well detected by SAR or visible images analysis.

3.3. Evolution of Inverted $\sigma_0$ During the Oil Spill

Using the method of inversion of waveform, we reprocess all the Jason-1 (pass 015) and Jason-2 (pass 204) altimeter data during the DWH spill to show the evolution of $\sigma_0$ during the oil spill. Figures 10a and 10b present the evolution of inverted Ku-band $\sigma_0$ for Jason-2 (from cycles 066 to 075) and Jason-1 (from cycles 306 to 314), respectively. For each cycle, the mean backscatter for the samples not covered by oil in the ERMA analysis has been subtracted to enhance the local impact of oil spill on backscatter. The red and white cross-hatched regions represent the collocated and coincident ERMA thick and thin oil covers within one day of altimeter measurements, respectively. The mean ECMWF and altimeter wind speed are also given in the figure. The rain flagged samples in the SGDR have been discarded from the analysis.

At low wind speed ($<3 \text{ m s}^{-1}$), the presence of oil either thin or thick is always associated with strong local increase of surface backscatter as shown in Jason-2 cycles 67, 69, and 71, and Jason-1 cycles 310 and 312. Given the lower resolution and the uncertainties of the thickness analysis of the ERMA fields, thicker oil corresponds to larger $\sigma_0$ enhancement than that for thin oil. Locally, the $\sigma_0$ increase can exceed 10 dB. Within the oil-covered zones, the large $\sigma_0$ variation, i.e., the notable attenuation of surface roughness, reflects the variation of oil thickness. Compared with the ERMA analysis, the altimeters give a more detailed description of the oil thickness distribution.
At moderate winds (3–6 m s⁻¹), high agreement between oil cover and \( \sigma_0 \) increase is shown in Jason-2 cycles 70, 72, 74, and 75 and Jason-1 cycles 306, 309, 311, and 314. Although the \( \sigma_0 \) increase within the oil spill is more limited than that at low wind, it can still reach 2 dB. Moreover, the variation of the \( \sigma_0 \) is larger within thick oil cover than that within thin oil. At higher winds (larger than 6 m s⁻¹), for Jason-2 cycle 66, 68, and 73 and Jason-1 307, 308, 309, and 313, the effect of oil on the \( \sigma_0 \) is only detectable within thick oil for the Jason-1 cycles 307 and 208. The variation of \( \sigma_0 \) exceeds 1 dB where the oil thickness is large. For most cycles, the \( \sigma_0 \) variations induced by wind variability are of the same order of magnitude as the ones caused by the spill.

To quantify the effect of oil on surface backscatter, the mean inverted Ku-band and C-band \( \sigma_0 \) distributions computed as a function of ECMWF wind speed and ERMA oil cover are shown in Figures 11 and 12,

Figure 8. Repositioned Jason-1 (a) Ku-band and (b) C-band waveforms for pass 015 cycle 310 (1 June 2010 18:15 UTC). The color scale represents the linear backscattered waveform power. (c) Off-nadir angles from the 1 Hz MLE4 estimator (red line) and inferred from the waveforms plateau slope (black line). (d) Ku-band and C-band MLE-4 \( \sigma_0 \) (red and black lines) and mean along-track inverted Ku-band and C-band \( \sigma_0 \) (blue and green lines). The dashed green and red line represent the limits of the ERMA thin and thick oil cover within the altimeter swath.
respectively. The means of $\sigma_0$ are listed in Table 1. The mean along-track $\sigma_0$ has been considered because its resolution is of the same order as the ERMA fields. At low wind speeds ($<3\text{ m s}^{-1}$), the distribution of $\sigma_0$ at both Jason-2 and Jason-1 Ku-band and C-band $\sigma_0$ (Figures 11 and 12a, and 12d) are significantly shifted toward higher values for thick oil. The mean $\sigma_0$ increase is similar for both Ku and C bands in the order of 1.0–3.5 dB for thick oil (Table 1). For thin oil, the shift toward higher value is smaller than that for thick oil for both Ku and C bands in the order of 0.9–2.9 dB.

For moderate winds (3–6 m s$^{-1}$), (Figures 11 and 12b, and 12e), there is a clear shift of the Ku-band and C-band $\sigma_0$ distributions toward larger values, especially for associated with higher $\sigma_0$ increase at both Ku and C bands while the oil thickness has no significant impact on Jason-2 $\sigma_0$. At winds larger than 6 m s$^{-1}$, the Jason-1 and Jason-2 Ku-band $\sigma_0$ (Figures 11 and 12c, and 12f) distributions for thick oil are slightly shifted toward higher values with a mean increase of 0.2–0.5 dB while the C-band $\sigma_0$ is not affected. There is also no detectable impact of thin oil on Jason-1/2 Ku-band and C-band backscatter.
Figure 10. Inverted high-resolution Ku-band $\sigma_0$ (in dB). The mean $\sigma_0$ outside the oil spill has been subtracted from each cycle to enhance the impact of the oil spill. The coincident and collocated ERMA thick and thin oil spill cover within the altimeter swath are represented as red and white cross-hatching, respectively. The mean ECMWF and altimeter wind speeds (m s$^{-1}$) are given for each cycle in the first and second row respectively. (a) Jason-2 pass 204 and cycles 066–075 (every 10 days from 25 April 2010 to 24 July 2010). (b) Jason-1 pass 015 and cycles 306–314 (every 10 days from 23 April 2010 to 24 July 2010). The white zones correspond to rain flagged data.

Figure 11. Histogram of Ku-band $\sigma_0$ for (a–c) Jason-2 pass 204 cycles 66–75 and (d–f) Jason-1 pass 015 cycle 306–314. The $\sigma_0$ is shown as a function of the oil cover and wind speed: wind < 3 m s$^{-1}$ (Figures 11a and 11d), 3 < wind < 6 m s$^{-1}$ (Figures 11b and 11e), and wind > 6 m s$^{-1}$ (Figures 11c and 11f).
The off-nadir angle is a good estimator of the waveform distortion and the presence of strong inhomogeneity of surface backscatter within the altimeter footprint. The distributions and mean of the absolute value of the off-nadir angle as a function of wind speed and oil cover are presented in Figure 13 and Table 2. At low wind speeds, the distributions and the mean values imply that both Jason-1 and Jason-2 waveforms are notably distorted within oil-covered zones. For Jason-2, the mean off-nadir angle strongly increases from 0.032 deg$^2$ for no oil to 0.047 deg$^2$ and 0.064 deg$^2$ for thin and thick oil (see Table 2), indicating larger inhomogeneity of the surface backscatter. For Jason-1, the mean off-nadir angle increases from 0.069 deg$^2$ for no oil to 0.14 and 0.23 deg$^2$ for thin and thick oil. The bin averaging of the waveform plateau region and the associated higher noise level explains the higher sensitivity of Jason-1 to waveform distortion. Hence, the shift of off-nadir angle distribution for Jason-1 (Figure 13c) is more significant than that for Jason-2 (Figure 13a). At low wind, the sea surface short waves are small and the roughness is low. The surface backscatter is high and small variations of surface roughness translates into large variations of surface backscatter [Kudryavtsev et al., 2012]. The presence of film on the surface leads to strong inhomogeneities of surface backscatter and thus high waveform distortion.

At moderate and higher winds, the impacts of oil thickness on Jason-1/2 off-nadir angle are similar with each other. For 3–6 m s$^{-1}$ winds, Jason-2 (Jason-1) off-nadir angle increases from 0.015 (0.12) deg$^2$ to 0.025 (0.025) deg$^2$ for thin oil and 0.027 (0.025) deg$^2$ for thick oil. Note that the mean off-nadir value even for thick oil is lower than that at low wind for oil free regions. When the wind increases, short wave grows and changes of surface roughness leads to smaller changes of surface backscatter and thus smaller inhomogeneity of the surface backscatter and smaller waveform distortion than that at low winds.

### Table 1. Mean $\sigma_0$ (in dB) as a Function of Wind Speed and Oil Cover

<table>
<thead>
<tr>
<th>Wind Speed</th>
<th>Ku Band</th>
<th>C Band</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No Oil</td>
<td>Thin Oil</td>
</tr>
<tr>
<td>Jason-2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0–3 m s$^{-1}$</td>
<td>16.3</td>
<td>17.2</td>
</tr>
<tr>
<td>3–6 m s$^{-1}$</td>
<td>14.5</td>
<td>14.9</td>
</tr>
<tr>
<td>&gt;6 m s$^{-1}$</td>
<td>13.3</td>
<td>13.2</td>
</tr>
<tr>
<td>Jason-1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0–3 m s$^{-1}$</td>
<td>18.4</td>
<td>21.3</td>
</tr>
<tr>
<td>3–6 m s$^{-1}$</td>
<td>15.1</td>
<td>15.5</td>
</tr>
<tr>
<td>&gt;6 m s$^{-1}$</td>
<td>14.1</td>
<td>14.2</td>
</tr>
</tbody>
</table>

4. Discussion and Summary

Surface films of natural or artificial origin damp short wind waves [Cox and Munk, 1954]. This damping of the capillary and short gravity waves by surface film produces dark slick signatures in SAR imagery and large contrast in sun-glitter imagery, bright and dark depending upon the local solar geometry [Hu et al., 2009; Kudryavtsev et al., 2012]. For
altimeter, specular reflection dominates and can produce bright patches or $\sigma_0$ bloom. Interpretation can follow the expected slope variance reduction \cite{Kudryavtsev2005} based on \cite{Ermakov1992} surface slick elasticity model. Under light winds ($< 3$ m s$^{-1}$), short gravity waves can be totally suppressed, resulting in $\sigma_0$ drops in SAR images and very large $\sigma_0$ increases at nadir in altimeter data \cite{Tournadre2006}. At low winds, small changes of wind speed and/or surface film elasticity (i.e., oil thickness) translate into large variations of specular reflection at small scale (but little Bragg scattering variations), causing significant altimeter waveform distortion.

With wind increasing, the background sea surface roughness becomes more homogeneous and the altimeter waveforms are less distorted. Moreover, the damping of capillary waves by surface film decreases \cite{Kudryavtsev2012}. At higher winds, only high elasticity films significantly dampen the shorter capillary waves and only is the Ku-band altimeter (i.e., the shorter capillary waves) significantly affected by film as it would require larger elasticity to dampen the longer C-band capillary waves.

Few studies focus on exploring the effect of oil slicks on satellite altimeter waveforms and $\sigma_0$. Lack of collocated and coincident information between oil spill and altimeter data limited the investigation to mainly theoretical modeling studies. Taking advantage of the large data set acquired during the DWH oil spill accident, we quantify the effect of oil slicks on altimeter data. The high-resolution $\sigma_0$ estimated by the waveform inversion method of \cite{Tournadre2011} is used to illustrate the effects of oil slick presence on surface $\sigma_0$. We collocated the Jason-1/2 altimetry data with SAR/MODIS imagery and ERMA oil cover data set to analyze the distortion of 20 Hz high-rate waveforms, surface $\sigma_0$ and off-nadir angle as a function of wind speed.

The $\sigma_0$ always increases within slicks, due to the attenuation of short surface waves by surface film. At low winds, both frequencies (Ku and C bands) of Jason-1 and 2 $\sigma_0$ distributions are shifted toward higher values in oil-covered regions and the shift is more pronounced for thicker oil (Figure 11a, 11d, 12a, and 12d). The increase of Ku-band and C-band $\sigma_0$ reaches 10 dB for thick oil (Figure 3). Jason-1/2 Ku-bands and C-bands show similar significant response to the thick oil (mean increase of 1.0–3.5 dB) and higher than that to thin oil (mean increase of 0.9–2.9 dB) (Table 1). Furthermore, the modulation of altimeter data

![Figure 13. Histogram of off-nadir angle as a function of oil cover and wind speed for (a-c) Jason-2 pass 204 cycle 66–75 and (d-f) Jason-1 pass 015 cycle 306 to 314: wind $< 3$ m s$^{-1}$ (Figures 13a and 12d), 3 $< \text{wind} < 6$ m s$^{-1}$ (Figures 13b and 12e), and \text{wind} $> 6$ m s$^{-1}$ (Figures 13c and 12f).](image-url)

<p>| Table 2. Mean Off-Nadir Angle (in deg$^2$) as a Function of Wind Speed and Oil Cover |
|---------------------------------|----------------|----------------|----------------|</p>
<table>
<thead>
<tr>
<th>Wind Speed</th>
<th>No Oil</th>
<th>Thin Oil</th>
<th>Thick Oil</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Jason-2</td>
<td>0–3 m s$^{-1}$</td>
<td>0.032</td>
<td>0.047</td>
<td>0.064</td>
</tr>
<tr>
<td></td>
<td>3–6 m s$^{-1}$</td>
<td>0.015</td>
<td>0.025</td>
<td>0.027</td>
</tr>
<tr>
<td></td>
<td>&gt;6 m s$^{-1}$</td>
<td>0.010</td>
<td>0.012</td>
<td>0.027</td>
</tr>
<tr>
<td>Jason-1</td>
<td>0–3 m s$^{-1}$</td>
<td>0.069</td>
<td>0.14</td>
<td>0.23</td>
</tr>
<tr>
<td></td>
<td>3–6 m s$^{-1}$</td>
<td>0.012</td>
<td>0.022</td>
<td>0.025</td>
</tr>
<tr>
<td></td>
<td>&gt;6 m s$^{-1}$</td>
<td>0.012</td>
<td>0.024</td>
<td>0.021</td>
</tr>
</tbody>
</table>
appears to be significantly more sensitive to film thickness than those of SAR and visible data. With the increase of wind speed, the impact of oil on $\sigma_0$ decreases for both frequencies. The difference of the effects between thick and thin oil becomes less pronounced due to the uncertainties of oil thickness analysis from SAR and visible imagery. Under moderate wind, the effect of oil on Jason-1/2 Ku-band $\sigma_0$ reaches 2 dB and can still be of the order of 1 dB for winds larger than 6 m s$^{-1}$ (Figure 10). With increasing winds, the impact of oil on C-band $\sigma_0$ becomes smaller than that at Ku band in good agreement with theoretical work by Kudryavtsev et al. [2012].

The analysis of the waveform distortion shows that at low winds, the off-nadir angle could be used as an additional factor to monitor the oil slicks and help the validation of oil thickness estimates. At moderate and higher winds, although the waveforms are more distorted within oil-covered regions, the values of the off-nadir angle are smaller than the one measured at low winds over oil free regions, which limits their potential use for spill detection.

Surface film causes $\sigma_0$ bloom in altimeter data and Jason-1/2 altimeter signal is more sensitive to oil thickness than SAR data. In short, altimeter data can certainly be used as a complementary data set to validate and delineate thick oil cover. The $\sigma_0$ inversion method throws a light on using airborne and satellite altimetry data for oil spill monitoring.

Appendix A: Altimeter Waveforms Inversion

The altimeter waveform inversion is described in detail in Tournadre et al. [2011] and is here summarized. Assuming that the distribution of the sea surface roughness and of the elevation are homogeneous over the altimeter footprint, the backscatter coefficient can be expressed as a convolution product of the radar antenna beam pattern and the joint probability of sea surface slope and elevation.

\[
\sigma_r = \frac{\pi^2 H^2 |R(0)|^2 \sigma_r}{2 \sigma_p} \int_0^\infty e^{-\frac{x^2}{2\sigma_p^2}} dx
\]  

where $t$ is the time, $x = ct/2$ is the distance between the surface and the antenna, $u = (H/\psi)^2/2$ is the ground range, $H^0$ and $H'$, defined by $H^0 = H^0/(1+H/a)$ and $H' = H/(1+H/a)$, are the reduced and extended satellite heights, $H$ being the satellite altitude and $a$ the earth’s radius; $R(0)$ is the Fresnel coefficient at zero incidence, $u_0$ is defined by $u_0 = (H/\psi_0)^2/2$, with $\psi_0 = \psi_H / \sqrt{8 \ln 2}$, $\psi_H$ being the two-way half-power antenna beam width. $\sigma_p$ is defined by $\sigma_p = \sqrt{\sigma_s^2 + \sigma_H^2}$; $h$ is the rms wave height and $\sigma_H$ is the mean surface backscatter coefficient defined as a function of the rms of the wave slopes $(s_x$ and $s_y$ in two orthogonal directions and $\rho_{xy}$ is the correlation coefficient of the wave slopes along this two axes by $\sigma_0 = (2 s_x s_y \sqrt{1 - \rho_{xy}})^{-1}$.

Assuming that the wave height is homogeneous over the altimeter footprint and that $\sigma_0$ is modulated by short scale variations, the echo waveform (A1) becomes

\[
\sigma_0(t) = \frac{1}{\sigma_r} \int_0^\infty \sigma_i(u, \theta) e^{-\frac{ct}{2\sigma_p}} du d\theta
\]  

where $\sigma = \frac{\pi^2 H^2 |R(0)|^2 \sigma_i}{2 \sigma_p}$ is a normalization coefficient, $\theta$ is the azimuth, $u$ is the range, $c$ is the speed of light, and $\sigma_i$ is the surface backscatter.

Let us consider a group of $N$ measured waveforms $w_i$ and the surface $\sigma_i$ on a regular grid $\{x_i, y_i\}$, using equation (A2), the $j$th element of the $i$th waveform $w_{ij}$ can be expressed in a discrete form as the sum of the $\sigma_{ij}$ whose range is between the range limits $\{u_j, u_{j+1}\}$ of bin $j$,

\[
w_{ij} = \sum_k \sum_l \sigma_{ij} \sigma_{kl} e^{-\frac{u_{ij}}{2\sigma_p}} (1 + \text{erf} \left( \frac{u_j}{\sqrt{2\sigma_p}} \right))
\]  

where the range $u_{ij}$ satisfies.
In a matrix form, the group of waveform \( \{ w_j, j = 1..N \} \) is expressed as \( W = A S \) (A6), where \( S \) is the matrix of the mean left/right surface backscatter (because of the left/right symmetry of the altimeter imaging process) and \( A \) is the altimeter imaging matrix that depends only on the altimeter geometry and can be easily computed using the range equation (A4). The imaging matrix can be easily computed by simple geometry. Let \( X^i \) be a surface grid element of area \( dx \times dy \) centered on \( x_i, y_i \). The coefficient \( a_{ijkl} \) of the imaging matrix \( A \) is equal to the surface of intersection between the grid element and the annulus centered at \( x^i, y^i \) and radii \( r_i \) and \( r_{i+1} \) (i.e., the range of bin \( i \)).

\[
a_{ijkl} = \int_{y_{i-1}}^{y_i} \int_{x_{ij-1/2}}^{x_{ij+1/2}} \left[ f_1(y) - f_2(y) \right] dy 
\]

where

\[
f_1(y) = \min\left( \sqrt{r_{i-1}^2 - (y - y^i)^2}, x_j + \frac{dx}{2} \right) 
\]

\[
f_2(y) = \max\left( \sqrt{r_{i}^2 - (y - y^i)^2}, x_j - \frac{dx}{2} \right) 
\]

The resolution of the surface backscatter grid has been chosen as the distance between two consecutive HR waveforms (290 m for Jason). The minimum number of waveforms to be considered is constrained by the width of the image of a nadir point in the waveform space that is about 3 seconds of data or 60 waveforms. In practice, \( N \) has been fixed to 75. For such grids, the linear system of equations (A6) is over-determined and can be inverted using pseudo-Moore-Penrose inverse \( A^+ \) computed using singular value decomposition [Penrose, 1955].

\[
S = A^{-1} W 
\]

