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## Novel Observation of Isospin Structure of Short-Range Correlations in Calcium Isotopes

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**Authors**

D. Nguyen, Z. Ye, Lawrence Weinstein, X. Zheng, P. Zhu, R. Zielinski, et al., and Jefferson Lab Hall A Collaboration

**Novel observation of isospin structure of short-range correlations in calcium isotopes**

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Short-range correlations (SRCs) have been identified as being responsible for the high-momentum tail of the nucleon momentum distribution,  $n(k)$ . Hard, short-range interactions of nucleon pairs generate the high-momentum tail and imprint a universal character on  $n(k)$  for all nuclei at large momentum. Triple coincidence experiments have shown a strong dominance of  $np$  pairs, but these measurements involve large final-state interactions. This paper presents the results from Jefferson Lab experiment E08014 which measured inclusive electron scattering cross section from Ca isotopes. By comparing the inclusive cross section from  $^{48}\text{Ca}$  to  $^{40}\text{Ca}$  in a kinematic region dominated by SRCs we provide a new way to study the isospin structure of SRCs.

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## I. INTRODUCTION

The naïve nuclear shell model has guided our understanding of nuclear properties for 60 years and it is still appealing as a predictive and illustrative nuclear model. This model, with nucleons moving in an average mean-field generated by the other nucleons in the nucleus, provides a quantitative account of a large body of nuclear properties. These include shell closures (“magic numbers”), the foundation of which is the appearance of gaps in the spectrum of single-particle energies [1].

The shell model is not without certain deficits which arise from what are generally called correlations—effects that are beyond mean-field theories such as long-range correlations associated with collective phenomena: giant resonances, vibrations, and rotations. In addition, electron-nucleus and nucleon-nucleus scattering experiments have unambiguously shown large deviations from the shell-model predictions, arising from the occurrence of strong short-range nucleon-nucleon correlations. These two-nucleon short-range correlations (2N-SRC) move particles from the shell-model states to large excitation energies and generate a high-momentum tail in the single particle momentum distribution. Consequently, over a large range in  $A$  the number of protons found in the valence shells orbitals is significantly less than expected, typically 60–70% of the predicted shell-model occupancy [2,3].

Inclusive experiments are able to isolate the 2N-SRC through selective kinematics: working at large momentum transfer [ $Q^2 \geq 1.5$  (GeV/c) $^2$ ] and small energy transfer ( $\nu \leq \frac{Q^2}{2m}$ ), corresponding to  $x = \frac{Q^2}{2m\nu} > 1$ , where  $m$  is the mass of the

proton. In these kinematics, inelastic scattering is minimized and quasielastic scattering requires that the struck nucleon have a nonzero initial momentum, as scattering at  $x > 1$  is kinematically forbidden for a stationary nucleon [4–6]. By selecting sufficiently large  $x$  and  $Q^2$ , the minimum initial nucleon momentum can be set above the Fermi momentum, dramatically suppressing the contribution from mean-field nucleons and isolating scattering from 2N-SRCs. It was through inclusive experiments [7–10] that 2N-SRCs were first revealed by the appearance of predicted plateaus [4] in the  $A/{}^2\text{H}$  per-nucleon cross-section ratio of nuclei to the deuteron. The height of the plateau is related to probability of finding a 2N-SRC in nucleus  $A$ , relative to the deuteron, indicating that  $\sim 20\%$  of the protons and neutrons in medium-to-heavy mass nuclei have momenta greater than the Fermi momentum  $k_F \simeq 250$  MeV/c [9]. The bulk of these nucleons do not arise in a shell-model description as they are the result of brief short-range interaction among pairs of nucleons giving rise to large relative momenta and modest center-of-mass motion,  $k_{\text{c.m.}} < k_F$  [4].

The isospin dependence of 2N-SRCs has been determined via  $A(p, p'pN)$  [11,12] and  $A(e, e'pN)$  [13–15] reactions in which the scattered particle (either a proton or an electron) is measured in coincidence with a high-momentum proton. The struck proton’s initial momentum, reconstructed assuming plane wave scattering, is approximately opposite that of the second high-momentum nucleon. These measurements exhibit a dominance of  $np$  pairs over  $pp$  pairs for initial nucleon momenta of 300–600 MeV/c which has been traced to the tensor part of the  $NN$  interaction [16–20]. These triple-coincidence experiments are sensitive to the isospin structure

of the SRC through direct measurement of the final-state nucleons. Because the signature of large back-to-back momenta is also consistent with striking a low-momentum nucleon which rescatters, there are large contributions from final-state interactions (including charge exchange) that need to be accounted for in comparing  $pp$  and  $np$  pairs [13–15]. Isospin dependence has never been established in inclusive scattering,  $A(e, e')$  until now.

We present here new  $A(e, e')$  measurements performed as part of Jefferson Lab experiment E08-014 [21]. Initial results on the search for three-nucleon SRCs in helium isotopes were published in Ref. [22]. The present work focuses on a measurement of the isospin dependence of 2N-SRCs in the cross-section ratio of scattering from  $^{48}\text{Ca}$  and  $^{40}\text{Ca}$ . The excess neutrons in  $^{48}\text{Ca}$  change the relative ratio of potential  $pp$ ,  $np$ , and  $nn$  pairs, but the impact on the cross section depends on whether the generation of high-momentum pairs is isospin independent or  $np$  dominated. This can be illustrated by making a very simple estimate. As a starting point, we take the fraction of nucleons in SRCs to be identical for these two targets, based on the observation of an  $A$ -independent value of  $a_2$ , the  $A/{}^2\text{H}$  cross-section ratio for  $1.5 < x < 2$ , for heavy nuclei [7, 10]. In the case of isospin-independent SRCs, protons and neutrons will have the same probability of appearing at momenta above  $k_F$ , giving a cross-section ratio of  $\frac{\sigma_{^{48}\text{Ca}}/48}{\sigma_{^{40}\text{Ca}}/40} = \frac{(20\sigma_{ep}+28\sigma_{en})/48}{(20\sigma_{ep}+20\sigma_{en})/40} \approx 0.93$  taking  $\sigma_{ep}/\sigma_{en} \approx 2.5$ , corresponding at the kinematics of this experiment. If SRCs are dominated by  $np$  pairs, then the cross-section ratio would be unity for isoscalar nuclei and slightly lower for nonisoscalar nuclei [23–26]. A more detailed cross-section model is presented later and used to interpret the data.

## II. EXPERIMENTAL DETAILS

Jefferson Lab experiment E08-014 [21] ran during the Spring of 2011. A 3.356-GeV continuous wave electron beam was directed onto a variety of targets, including  ${}^2\text{H}$ ,  ${}^3\text{He}$ ,  ${}^4\text{He}$ ,  ${}^{12}\text{C}$  and targets of natural calcium (mainly  $^{40}\text{Ca}$ ) and an enriched target of 90.04%  $^{48}\text{Ca}$  (referred to as the  $^{40}\text{Ca}$  and  $^{48}\text{Ca}$  targets, respectively). The scattered electrons were detected at angles of  $\theta = 21^\circ, 23^\circ, 25^\circ$ , and  $28^\circ$ , though no calcium data were taken at  $28^\circ$ . The data presented here cover a kinematic region of  $1.3 < Q^2 < 1.9$  (GeV/c) $^2$  and  $1 < x < 3$ .

The inclusive scattered electrons were detected using two nearly identical left and right high-resolution spectrometers (LHRS and RHRS). The spectrometers consisted of a set of three quadrupole magnets and a dipole magnet which transported the events from the target to the detector plane. Each spectrometer was equipped with a detector package consisting of two vertical drift chambers (VDC) for tracking information [27], a gas Cerenkov counter [28] and two layers of lead glass calorimeters for particle identification, and two scintillator counter planes for triggering [29].

The accumulated charge for each experimental run was measured by beam current monitors with an uncertainty of 0.5%, based on the difference in the calculated charge using two sets of beam calibration parameters. The dead time due to the inability of the data acquisition system to accept new

triggers while processing an earlier event was corrected for each run using the trigger scaler information. The main trigger for data collection required a coincidence of signals from two scintillator planes and the Cerenkov, which had a local inefficiency region. A sample of events were taken with a second trigger which did not require the Cerenkov signal, allowing for continuous measurement of the inefficiency. The correction was applied to the measured yield in each  $x$  bin for every kinematic setting. Pions were rejected (with negligible remaining pion contamination) by applying additional cuts on both the Cerenkov counter and the lead glass calorimeter with efficiencies of 99.5% and 99.6% respectively, with a tracking efficiency of 98.5%. Detailed descriptions of the experimental setup and data analysis can be found in Refs. [30, 31].

The position and angle of the scattered electrons are measured at the VDCs. These are used to reconstruct the angle and momentum of the scattered electron using reconstruction matrices which parametrize the transformation between electron trajectory at the target and the VDCs. These were determined by a fit to special data runs where the particle angle or momentum were determined by taking data in over-constrained kinematics (e.g., elastic scattering) to define the momentum or using a collimator with small holes at the entrance to the first HRS magnet [29] to define the scattering angle. For the left HRS, the reconstruction matrix was fitted to data taken from the previous experiment [32] which had the same spectrometer and magnet settings as this experiment. The magnet tune for the RHRS had to be modified because the third quadrupole could not run at the desired field, and lack of a complete set of calibration data for to fit led to a reduced resolution in the RHRS. The reduced resolution affected the extraction of the cross section at large  $x$  values where the cross section falls extremely rapidly, requiring a larger correction. Because the RHRS was typically taking data in the same kinematics as the LHRS, we used only the data from the LHRS except for the  $21^\circ$  data, where the largest  $x$  values were measured only in the RHRS. For this setting we included the ratios from the RHRS, as the smearing has a negligible impact on the cross-section ratios in the region where the ratio is flat.

The yield for the experiment was simulated using a detailed model of the HRS optics and acceptance, with events generated uniformly and weighted by a radiative cross-section model [31, 33]. The model used a  $y$ -scaling fit [34, 35] for quasielastic cross section (initially based on previous data, and iteratively updated to match the extracted cross sections from this experiment) and a global fit [36] for the inelastic contribution. The Born cross section was extracted by taking the model cross section and correcting it by the ratio of measured to simulated yield. Comparing the results extracted with the final model and the model before being adjusted to match our data indicated a model uncertainty of 0.5% in both the absolute cross sections and the target ratios.

The cross-section ratio obtained from the enriched and natural calcium targets was then corrected to yield  $^{48}\text{Ca}/^{40}\text{Ca}$  ratio, based on the isotopic analysis of the targets. No correction was applied to the natural calcium, which was over 99.9%  $^{40}\text{Ca}$ . The enriched calcium target was 90.04%  $^{48}\text{Ca}$  and 9.96%  $^{40}\text{Ca}$ , by number of atoms. Using the measured  $^{40}\text{Ca}$  cross section, we correct for the  $^{40}\text{Ca}$  contribution in

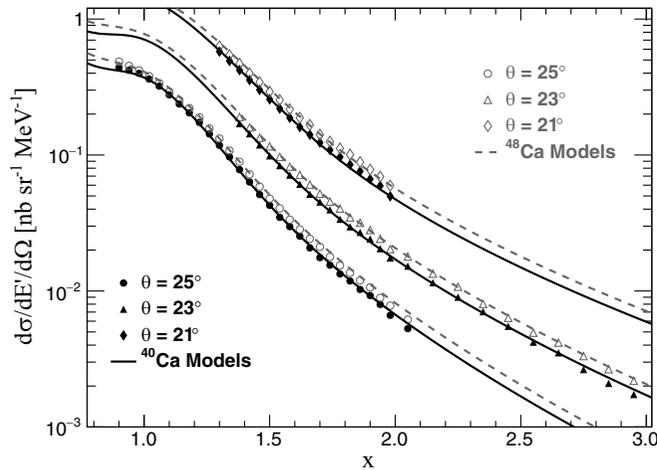


FIG. 1.  $^{48}\text{Ca}$  and  $^{40}\text{Ca}$  cross sections for three different angle settings, along with the cross-section model used in the analysis. Uncertainties shown include statistical and point-to-point systematic uncertainties; an additional normalization uncertainty of 2.7% for  $^{40}\text{Ca}$  and 3.0% for  $^{48}\text{Ca}$  is not shown.

the enriched target to extract the  $^{48}\text{Ca}$  cross section. The correction is typically 0.5–1.5%.

### III. RESULTS

The measured cross sections are presented in Fig. 1. For the cross sections, the point-to-point systematic uncertainty is estimated to be 1.9%, with dominant contribution coming from the acceptance (1.5%), radiative corrections (1%), and the model dependence of the cross-section extraction (0.5%). In addition, there is an overall normalization uncertainty of 2.7%, coming mainly from the acceptance (2%), radiative correction (1%), and target thickness (1%). These are the uncertainties for the  $^{40}\text{Ca}$  target. The dilution correction used to extract the  $^{48}\text{Ca}$  cross section increases these, giving 2.1% point-to-point and 3.0% normalization uncertainties.

The point-to-point uncertainty due to the acceptance was determined by systematically selecting five different sets of acceptance cuts. The uncertainty was taken to be the variation in the extracted cross sections corresponding to these cuts, which was consistent with previous estimates of the HRS acceptance. The cross-section model in this analysis was iterated three times. The variation in the extracted cross sections using different iterated models was assigned as the point-to-point uncertainty for the model dependence. Radiative corrections were applied using the prescription described in Ref. [37], with uncertainties that account for limitations of the procedure and uncertainty in the energy loss and radiation length of the target material.

The per nucleon cross-section ratio of  $^{48}\text{Ca}$  to  $^{40}\text{Ca}$  is presented in Fig. 2 for each of the three scattering angles and in Fig. 3 after combining of the data sets. Because the cross section and experimental conditions are very similar for the two targets, many of the uncertainties in the cross sections cancel or are reduced in the ratio. The systematic uncertainty on the ratios is 0.9%, dominated by the model dependence

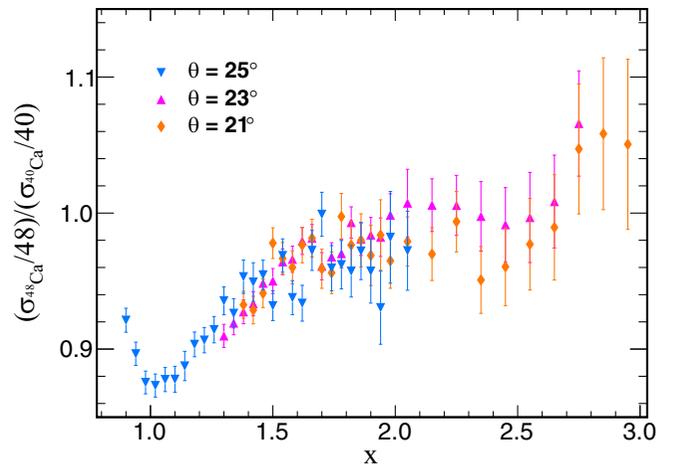


FIG. 2. Ratio of the cross section per nucleon for  $^{48}\text{Ca}$  and  $^{40}\text{Ca}$  for three scattering angles. Uncertainties shown include statistical and point-to-point systematic uncertainties; an additional normalization uncertainty of 1% is not shown.

in the extraction (0.5%), measurement of the beam charge (0.5%) and the radiative correction (0.5%). An additional 1% normalization uncertainty, associated with the uncertainty in the relative target thicknesses, is not shown. For Fig. 3, we combined the statistics of the individual sets (for three angles) and then apply the 0.9% point-to-point uncertainty (and 1% normalization uncertainty) to the result.

Note that the rise from  $x = 1$  to  $x = 1.6$  looks slightly different than it does for the ratios to  $^2\text{H}$  [7,10]. This is expected as the shape in the  $A/^2\text{H}$  ratios is driven by the deuterium cross section, which is narrowly peaked at and roughly symmetric about  $x = 1$ . The line in Fig. 3 indicates the value of  $R_{\text{SRC}}$ , the average in the plateau region:  $1.5 < x < 2$ . The fit gives  $R_{\text{SRC}} = 0.971(3)(6)(10) = 0.971(12)$  where the error contributions come from the point-to-point uncertainties, the

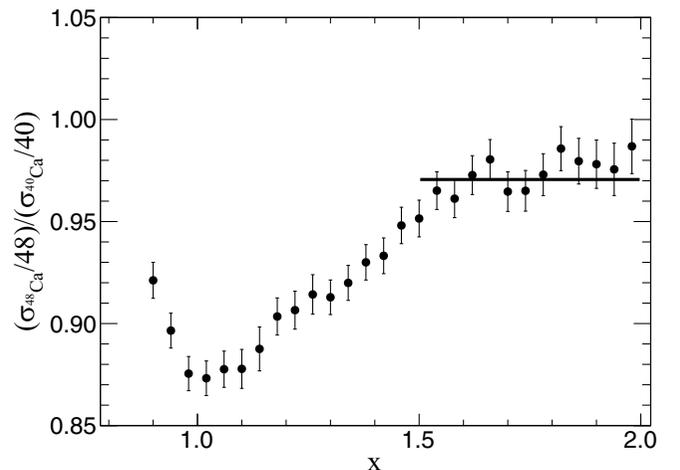


FIG. 3. Ratio of the cross section per nucleon for  $^{48}\text{Ca}$  and  $^{40}\text{Ca}$  combining all three data sets. A 1% normalization uncertainty is not shown. The line indicates the fit for the cross-section ratio in the SRC region

cut dependence of the extracted  $R_{\text{SRC}}$ , and the normalization uncertainty of the ratios. The cut dependence is taken to be the RMS scatter of  $R_{\text{SRC}}$  values fit separately to the three scattering angles for three different minimum  $x$  values,  $x_{\text{min}} = 1.5, 1.6, \text{ and } 1.7$ .

The observed value of  $R_{\text{SRC}} = 0.971(12)$  is more than three  $\sigma$  above the prediction for isospin independence ( $R_{\text{SRC}} = 0.930$  for these kinematics). So while inclusive scattering cannot isolate contributions from protons and neutrons, comparing calcium isotopes with significantly different  $N/Z$  values is sensitive enough to provide evidence for an enhancement of  $np$  pairs over  $pp$  and  $nn$  pairs.

#### IV. DISCUSSION

To quantitatively interpret this ratio in terms of relative  $np$ ,  $pp$ , and  $nn$  SRC contributions, and to compare these results to observable from previous measurements, we use a simple model to estimate the inclusive, exclusive, and two-nucleon knockout ratios in terms of a few parameters. We take the number of 2N-SRCs to be a product of the number of total pairs, the probability for any two nucleons to be close enough together to interact via the short-range  $NN$  interaction ( $f_{\text{sr}}$ ), and the probability that the  $NN$  interaction generates a high-momentum pair ( $p_{NN}$ ). The total number of  $np$ ,  $pp$ , and  $nn$  pairs are  $NZ$ ,  $Z(Z-1)/2$ , and  $N(N-1)/2$ , respectively. The fraction of nucleons at short distance,  $f_{\text{sr}}$ , depends on the nucleus and is assumed to be identical for  $nn$ ,  $np$ , and  $pp$  pairs. The probability that these nucleons generate high-momentum pairs,  $p_{np}$  and  $p_{pp} = p_{nn}$ , depends on the momentum range of the initial nucleons,  $\Delta P_i$ , defined by the experiment for coincidence measurements or by the kinematics in inclusive scattering. Given this, we can express the number of  $np$  and  $pp$  SRCs as:

$$N_{np} = NZ f_{\text{sr}}(A) p_{np}(\Delta P_i), \quad (1)$$

$$N_{pp} = Z(Z-1)/2 f_{\text{sr}}(A) p_{pp}(\Delta P_i). \quad (2)$$

While  $p_{np}$  and  $p_{pp}$  may depend strongly on  $\Delta P_i$ , we assume that their ratio has a much weaker dependence, as observed in Ref. [15], and so their ratio extracted from different measurements should be comparable. This leaves only  $f_{\text{sr}}(A)$  as an unknown. In comparing different observables on the same nucleus, e.g., taking the ratio of  $A(e, e'pp)$  to  $A(e, e'pn)$ ,  $f_{\text{sr}}(A)$  cancels out. In the limit of large nuclei, any given nucleon will be sensitive to short-range interactions with nucleons in some fixed volume, while the number of nucleons grows with  $A$ , suggesting that  $f_{\text{sr}}(A)$  should scale as  $1/A$ . With this assumption, our model produces a constant value of  $a_2$  for heavy isoscalar nuclei, consistent with the observation of approximate saturation [38]. Note that the result  $f_{\text{sr}}(A) \propto 1/A$  is derived assuming  $np$  dominance. Under the isospin-independent assumption,  $f_{\text{sr}}(A)$  must scale as  $1/(A-1)$ . For the comparison of  $^{48}\text{Ca}$  to  $^{40}\text{Ca}$ , the difference between these cases is less than 0.5%.

Within this model, we can calculate the number of  $pp$ ,  $np$ , and  $nn$  SRCs in the  $^{40}\text{Ca}$  and  $^{48}\text{Ca}$  targets. Each SRC pair contributes to the inclusive cross section in the SRC-dominated region based on the  $e$ - $N$  elastic cross section for the two

nucleons. In cross-section ratio, only the  $A$  dependence of  $f_{\text{sr}}(A)$  remains and the ratio depends only on the  $A$  dependence of  $f_{\text{sr}}(A)$  which is taken to scale as  $1/A$ . The cross-section ratio thus depends only on the ratio of electron-proton to electron-neutron elastic scattering, and on the ratio  $p_{np}/p_{pp}$ , the enhancement factor of  $np$  pairs to high momentum relative to  $pp$  (and  $nn$ ) pairs. The average value of  $\sigma_{ep}/\sigma_{en}$  is 2.55–2.60 for these kinematics, this model predicts the cross-section ratio to be 0.930 for isospin independence, and 0.972 for  $np$  dominance.

The observed cross-section ratio is significantly above the prediction for isospin-independent pairing. Taking into account its uncertainty, we find that  $p_{np}/p_{pp} > 2.9$  at the 95% confidence level, and  $p_{np}/p_{pp} > 1.6$  at the 99% confidence level, demonstrating  $np$  dominance using the isospin structure of the target, rather than the detected nucleons, to study the isospin structure.

Our prediction for the isospin-independent ratio neglects the difference between the size of the proton and neutron distributions in  $^{48}\text{Ca}$ . Based on the estimated charge radius [39] and a neutron skin [40], the RMS radii of the proton and neutron distributions are 3.5 fm and 3.7 fm, respectively. Relative to our model, which assumes a uniform radius of 3.6 fm, the proton (neutron) distribution is roughly 8.5% smaller (larger) in volume which will increase proton pairing and decrease neutron pairing by similar amounts. Because the  $pp$  and  $nn$  pairs contribute nearly equally to the  $x > 1$  cross section in  $^{48}\text{Ca}$ , the net impact on the cross section is a very small ( $<0.5\%$ ) increase in the  $^{48}\text{Ca}$  cross section. The contribution from  $np$  pairs, which dominate the cross section, will be decreased due to the reduced overlap between the proton and neutron distributions, providing a modest reduction to the  $^{48}\text{Ca}$  cross section. The net effect should be a decrease in the prediction of  $R_{\text{SRC}} = 0.930$  for the isospin-independent model, although the size of the effect is difficult to estimate precisely. However, taking  $R_{\text{SRC}} = 0.930$  as an upper limit, the indications for  $np$ -dominance seen in the data will be at least as significant as estimated above.

The ratio  $p_{np}/p_{pp}$  cannot be directly compared to the enhancement factor of  $\sim 10$  obtained in triple coincidence experiments [14,15], as it removes the contribution from simple pair counting. For example,  $^4\text{He}$  has four  $np$  pairs and only one  $pp$  pair, and thus one would expect  $np$  pairs to dominate, even if the generation of high-momentum pairs had no isospin dependence. Using our simple model we can extract  $p_{np}/p_{pp}$  from other measurements,  $A(e, e'pp)/A(e, e'pn)$  or  $A(e, e'p)/A(e, e'n)$ , allowing for a more direct comparison. As noted before,  $p_{np}$  and  $p_{pp}$  depend on the momentum of the struck nucleon in the initial-state SRC, while for the inclusive case, they correspond to an average over the momentum range probed in the scattering which depends on  $Q^2$  and the  $x$  range of the data. Because of this, the extracted enhancement factor for inclusive scattering corresponds to a range of momenta that should be similar, but not identical, to the momentum range selected in the coincidence knockout reactions.

Writing out the ratio of  $A(e, e'pp)/A(e, e'pn)$  in terms of  $p_{np}/p_{pp}$  allows us to take the observed ratios and extract the  $np$  enhancement factor. For  $^4\text{He}$  [15], the  $pp/np$  fraction is  $(5.5 \pm 3)\%$ , giving a one- $\sigma$  range of  $2.9 < p_{np}/p_{pp} < 10$ .

For  $^{12}\text{C}$ , the  $pp/np$  fraction is  $(5.6 \pm 1.8)\%$  leading to a one- $\sigma$  range of  $5.6 < p_{np}/p_{pp} < 11$ . The full expressions are provided in the Supplemental Material [41]. The triple-coincidence measurements quote their results in  $P_m$  (missing momentum) bins, which represent the reconstructed initial momentum of the struck nucleon [15]. We take the lowest  $P_m$  bins from the triple-coincidence measurements, covering momenta from 300–600 MeV/ $c$ , to more closely match the main contributions to the inclusive measurement. As noted above, these values are not exactly equivalent to the values extracted from the inclusive scattering, but they paint a consistent picture of significant  $np$  dominance in SRCs over a range of light and heavy nuclei.

## V. CONCLUSIONS

In conclusion, the per nucleon cross-section ratio of  $^{48}\text{Ca}/^{40}\text{Ca}$  is consistent with significant  $np$  dominance in the creation of SRCs. It shows an enhancement of  $np$  pairs over  $pp$  pairs at more than the three- $\sigma$  level.

This data provides the first evidence of  $np$  dominance from inclusive scattering, making use of the isospin structure of the target rather than the final  $NN$  pair. This approach avoids the significant corrections required to interpret triple-coincidence measurements, but does not provide a quantitative measure of the enhancement factor because of the small difference between isospin-independent and  $np$ -dominance

assumptions. A recent experiment measured the inclusive ratio for scattering from  $^3\text{H}$  and  $^3\text{He}$ , which is significantly more sensitive [42]. The  $^3\text{H}/^3\text{He}$  cross-section ratio is approximately 0.75 for isospin independence and 1 for  $np$  dominance, giving almost an order of magnitude more sensitivity than the  $^{48}\text{Ca}/^{40}\text{Ca}$  ratio, without having to make any assumption about the  $A$  dependence of  $f_{\text{sr}}(A)$  in comparing the two nuclei. A measurement of this inclusive cross-section ratio with comparable uncertainties may provide the best quantitative measurement of the enhancement of  $np$  pairs at high momentum.

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