Deeply Virtual Compton Scattering Cross Section at High Bjorken $\B$

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Deeply Virtual Compton Scattering Cross Section at High Bjorken $x_B$


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In this Letter, we present an experimental determination of the four complex helicity-conserving amplitudes of the $e^+e^-$ cross section at high values of the Bjorken variable $x_B$. DVCS is sensitive to the generalized parton distributions of the nucleon, which provide a three-dimensional description of its internal constituents. Using the exact analytic expression of the DVCS cross section for all possible polarization states of the initial and final electron and nucleon, and final state photon, we present the first experimental extraction of all four helicity-conserving Compton form factors (CFFs) of the nucleon as a function of $x_B$, while systematically including helicity flip amplitudes. In particular, the high accuracy of the present data demonstrates sensitivity to some very poorly known CFFs.

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TABLE I. Main kinematic variables for each of the nine \((Q^2, x_B)\) settings where the DVCS cross section is reported. \(E_b\) is the incident electron energy, \(E_q\) and \(-t_{\text{min}}\) correspond to a final state photon emitted parallel to \(q = k - k'\) at the nominal \(Q^2, x_B\) values listed. For each setting, the cross section is measured as a function of \(t\) (3 to 5 bins depending on the setting) and in 24 bins in \(\phi\). The accumulated charge, corrected by the acquisition dead time, is listed in the row labeled \(\int Q dt\). The last row of the table indicates the number of statistically independent measurements (bins) for each \(x_B\) setting, including helicity dependence.

<table>
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<tr>
<td>(x_B)</td>
<td>0.36</td>
<td>0.48</td>
<td>0.60</td>
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<tr>
<td>(E_b) (GeV)</td>
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<td>8.52</td>
<td>10.59</td>
<td>4.49</td>
<td>8.85</td>
<td>8.85</td>
<td>10.99</td>
<td>8.52</td>
<td>10.59</td>
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<tr>
<td>(Q^2) (GeV^2)</td>
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<td>3.60</td>
<td>4.47</td>
<td>2.70</td>
<td>4.37</td>
<td>5.33</td>
<td>6.90</td>
<td>5.54</td>
<td>8.40</td>
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<td>(E_q) (GeV)</td>
<td>4.7</td>
<td>5.2</td>
<td>6.5</td>
<td>2.8</td>
<td>4.7</td>
<td>5.7</td>
<td>7.5</td>
<td>4.6</td>
<td>7.1</td>
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<tr>
<td>(-t_{\text{min}}) (GeV^2)</td>
<td>0.16</td>
<td>0.17</td>
<td>0.17</td>
<td>0.32</td>
<td>0.34</td>
<td>0.35</td>
<td>0.36</td>
<td>0.66</td>
<td>0.70</td>
</tr>
<tr>
<td>(\int Q dt) (C)</td>
<td>1.2</td>
<td>1.7</td>
<td>1.3</td>
<td>2.2</td>
<td>3.7</td>
<td>5.7</td>
<td>6.4</td>
<td>6.4</td>
<td>18.5</td>
</tr>
<tr>
<td>Number of data bins</td>
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<td>912</td>
<td>480</td>
<td></td>
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correlating the transverse spatial and longitudinal momentum distributions of quarks and gluons inside the proton, leading to a sum rule for the separate contributions of quarks and gluons to the spin of the proton [1].

The \(e\)p scattering kinematics in the Bjorken limit define a preferred longitudinal axis (up to ambiguities of order \(t/Q^2\)). Light cone momenta \(P^\pm = (P^0 \pm P^z)/\sqrt{2}\) and light cone helicities of the external particles are defined with respect to this axis. The variables \(x \pm \xi\) are the light cone momentum fractions of the initial and final active quark. The variable \(\xi\) is kinematic: \(\xi \approx q/z(2 - x_B)\), whereas \(x\) is integrated from \(-1\) to \(1\) as a consequence of the implied quark loop. The experimental \(e\)p \(\to e\)\(\gamma\) scattering amplitude is the coherent sum of the Compton amplitude and the Bethe-Heitler (BH) amplitude, wherein the real photon is emitted by the incoming or the scattered electron, as illustrated in Fig. 1.

In this analysis of the Jefferson Lab Hall A experiment E12-06-114, we follow the Braun-Manashov-Müller-Pirnay (BMMP) formalism [6], wherein the longitudinal axis is defined in an event-by-event frame in which the three vectors \(q\) and \(q'\) are colinear. More generally, the light cone is defined by null vectors \(q^\prime\) and \(q - q^\prime/(1 - t/Q^2)\). In this reference frame, the leading four Compton amplitudes conserve the light cone helicity of the photons. The proton helicity dependence of the Compton amplitude is expressed through the definition of four chiral-even Compton form factors (CFFs) \((H_{++}, \tilde{H}_{++}, E_{++}, \tilde{E}_{++})\), which are convolution integrals of the four corresponding GPDs. Each CFF is associated with a unique nucleon-spinor matrix element of, e.g., \(\gamma^+, \gamma^+\gamma_5, \ldots\).

The reduction of the twelve Compton amplitudes to just four amplitudes, as first described in [3] is a profound simplification. Nonetheless in the range of \(Q^2\) and \(x_B\) currently accessible, the remaining eight chiral-odd photon helicity-flip Compton amplitudes, while small, cannot be completely neglected.

The HERMES Collaboration performed extensive measurements of single- and double-spin DVCS asymmetries [7–9]. The H1 [10] and ZEUS [11] Collaborations measured the DVCS cross section over a broad range of \(Q^2\) and \(W^2\) at low \(x_B\). The Jefferson Lab CLAS Collaboration has measured DVCS beam spin asymmetries and cross sections [12–14] and longitudinally polarized target asymmetries [15–17]. Recent experimental studies on DVCS show that the contributions of the chiral-even GPDs dominate the DVCS amplitude already at \(Q^2\) values as low as 1.5 GeV^2 [13,18,19]. However, dynamic terms involving a photon helicity flip are not negligible, even though they are nominally suppressed by powers of \((t, M^2)/Q^2\) [20].

This Letter reports the results of experiment E12-06-114, which ran in Hall A at Jefferson Lab in the fall of 2014 and in 2016. Concurrent data on \(e\)p \(\to e\)p\(\pi^0\) were published in [21], which also includes additional experimental and analysis details. Table I shows the nine kinematic settings in \(Q^2\) and \(x_B\) at which the DVCS cross sections were measured. For each setting, the data are binned in \(t\) and the azimuth \(\phi\) of the detected photon \(q'\) around the direction of \(q\), as defined by the “Trento convention” [22].

The longitudinally polarized electron beam impinged on a 15-cm liquid hydrogen target. The beam current was adjusted between 5 and 15 \(\mu\)A, depending on the kinematic setting, in order to maintain dead time below 5%. The Hall A Møller polarimeter measured an averaged beam polarization of 86 \pm 1%. The \(H(e, e'\gamma)X\) reaction was the main trigger of the data acquisition system. The scattered electron was detected by a coincidence signal between the scintillators and the Cerenkov detector of the left high-resolution spectrometer (HRS) [23]. The electron identification was further refined off-line by the use of a Pb-glass calorimeter in the HRS. The outgoing photon was detected by a dedicated highly segmented PbF\(_2\) electromagnetic calorimeter. The analog signal from each of the 208 calorimeter channels was recorded over 128 ns by 1 GHz digitizing electronics based on the analog ring sampler (ARS) chip [24,25]. Following an HRS electron trigger (level 1), calorimeter signal sampling was started. Waveform digitization was validated by a level-2 trigger.
which computed the sum of the signal from all channels in a 80 ns window. If a signal above a programmable threshold was found in the calorimeter, the digitization process took 128 μs; otherwise the ARS system resumed sampling after 500 ns. The level-2 trigger was based on a field-programmable gate array module, and was used only during high counting rate settings (> 1 kHz). For settings with low rates, all level-1 triggers were validated and waveforms digitized [21]. Off-line analysis of the calorimeter signals and regular energy calibrations resulted in an energy resolution of 3% at 7 GeV. Missing-mass reconstruction identified the nondetected proton (see Fig. 2). The time resolution between the electron and photon detections was better than 1 ns. The number of random coincidences was evaluated by analyzing events in a time window shifted with respect to the coincidence time of the HRS and calorimeter signals.

An important source of background was neutral-pion electroproduction events for which only one of the decay photons was detected. The number of one-photon events from π⁰ decays was estimated by a Monte Carlo simulation normalized bin by bin to the number of detected π⁰ → γγ events. The acceptance and resolution of the experiment were modeled by a GEANT4 simulation. The simulation included bin migration effects due to real and virtual radiation and the PbF₂ calorimeter energy resolution, as described in [19]. During the data taking, the first quadrupole of the HRS experienced the gradual failure of its cryogenic current lead. For the first part of the experiment, the faulty quadrupole could only be used at a reduced current supply. Before the fall 2016 data taking, that quadrupole was replaced by a room-temperature quadrupole providing a similar magnetic field. Optics calibrations data were taken to maintain the excellent resolution of the HRS. Effects on the spectrometer acceptance were taken into account for each kinematic setting and run period by

FIG. 2. Missing mass squared of the ep → eγX reaction for kinematic setting Kin-48-1, integrated over t and ϕ. Experimental data are shown in black. The subtraction of the accidental contribution (green) and photons from π⁰ decays (blue) yields the red histogram.
applying similar multidimensional cuts (R cuts, [26]) on both the experimental and simulated data.

Deep inelastic scattering data were taken simultaneously to the main DVCS data using an ancillary trigger for all kinematic settings, which allowed a monitor of the scattered electron detection efficiency and acceptance [21]. The total systematic uncertainty of the DVCS cross-section measurements includes the uncertainty on the electron detection and acceptance, the luminosity evaluation, the uncertainty on the photon detection, and the exclusivity. Radiative corrections are included in the analysis based on calculations of [27] and using the procedure described in detail in [21].

Figure 3 shows a sample of the cross section measured at each of the $x_B$ settings. See Supplemental Material [28] for the full set of data. The azimuthal dependence of the cross section is fit using the BMMP formalism [6], and the contribution from the BH-DVCS interference and DVCS contributions are shown along with the BH cross section. The BMMP calculation includes kinematic power corrections $\sim t/Q^2$ and $\sim M^2/Q^2$ that were proven to be important at these kinematics [20]. The cross section is expressed as a function of helicity-conserving CFFs ($H_{++}$, $H_{++}$, $E_{++}$, and $\tilde{E}_{++}$), longitudinal-to-transverse helicity-flip CFFs ($H_{0+}$, $\tilde{H}_{0+}$, $E_{0+}$, and $\tilde{E}_{0+}$), and transverse helicity-flip CFFs ($H_{-+}$, $\tilde{H}_{-+}$, $E_{-+}$, and $\tilde{E}_{-+}$). For each GPD label, the subscripts $\lambda$, $\lambda'$ refer to the light cone helicity of the initial (virtual) and final (real) photon, respectively. In this formalism, the light cone is defined by linear combinations of $q^\mu$ and $q'^\nu$. Our whole dataset has been fitted using this complete and consistent scheme, with the real and imaginary part of all these CFFs being the free parameters (a total of 24) of the fit. All kinematics bins in $Q^2$ and $\phi$ at constant $(x_B, t)$ are fitted simultaneously, however possible QCD evolution of the CFFs as functions of $Q^2$ is not considered.

While the number of fit parameters is large, the high accuracy of the data allows to simultaneously extract all the helicity-conserving CFFs with good statistical uncertainties. Figure 4 shows the real and imaginary part of all four helicity-conserving CFFs as a function of $x_B$ averaged over $t$. These results represent the first complete extraction of all helicity-conserving CFFs appearing in the DVCS cross section, including the poorly known $E_{++}$ and $\tilde{E}_{++}$. The state-of-the-art GPD parametrization KM15 [29] that reproduces worldwide DVCS data show a reasonable agreement but fail to describe $E_{++}$ and $\tilde{E}_{++}$ accurately.

As first demonstrated in [20] and described theoretically in [30], the measurement of the DVCS cross section at two or more values of the $ep$ center-of-mass energy $\sqrt{s}$ provides statistically significant separation of the real and imaginary parts of the BH-DVCS interference term as well as the DVCS$^2$ contribution in the cross sections for polarized electrons. A new analysis [31] of all previous JLab DVCS data followed a similar procedure, and obtained flavor-separated Compton form factors, after inclusion of our recent neutron DVCS data [32]. In the present analysis, realistic error bands on the chiral-even CFFs are obtained by explicit inclusion of higher-order terms (e.g., $\mathcal{H}_{0+}$, $\mathcal{H}_{-+}$, etc.) in the cross section fit, with these terms primarily constrained by inclusion of higher Fourier terms in the azimuthal variable $\phi$. Although the extracted values of the helicity-flip CFFs are largely statistically consistent with zero, the statistical correlations between all of the CFF values at fixed $x_B$ are essential to obtaining realistic experimental uncertainties. Figure 5 illustrates for setting $x_B = 0.60$ the values of CFFs as a function of $t$ obtained when the fit includes only the helicity-conserving CFFs (red points) and when both helicity-conserving and helicity-flip CFFs are included (black points). One can see that fitting only helicity-conserving CFFs significantly underestimates their uncertainties.
The sensitivity to the CFFs $\mathcal{E}$ and $\tilde{\mathcal{E}}$ illustrated in Fig. 4 arises from the $Q^2$-dependent kinematic factors weighting these terms relative to the contributions of $\mathcal{H}$ and $\tilde{\mathcal{H}}$. The KM15 model [29] includes only the $D$ term (support limited to $|x|<\xi$) in the $E$ GPD, and therefore vanishes at $x=\xi$, resulting in $\text{Im}[\mathcal{E}]=0$. For $\tilde{E}$, this model includes only the pion pole, via the $\gamma^*\gamma \to \pi^0$ amplitude, and thus the amplitude in this channel is also purely real. In contrast, the model of [33] for $\tilde{E}$ includes a valence quark contribution with support outside the $|x|<\xi$ bound and therefore produces a nonzero imaginary part of the $\tilde{E}$ CFF. Similarly, the chiral quark soliton model [33,34] produces a contribution to $\tilde{E}$ that while smaller in magnitude to the pion pole, is additive with opposite sign. This may explain the significant difference between our values of $\text{Re}[\tilde{\mathcal{E}}]$ and the KM15 model. GPDs $E$ and $\tilde{E}$ (summed over quark flavor $f$) to the axial and pseudoscalar form factors $G_A$ and $G_P$ of the proton:

$$\sum_f \int_{-1}^1 \left\{ \frac{E_f(x,\xi,t)}{\rho_f(x,\xi,t)} \right\} dx = \begin{cases} G_A(-t) \\ G_P(-t) \end{cases}.$$  (1)

These form factors, particularly $G_P$, are much less well known experimentally than the usual electromagnetic form factors $G_{E,M}$. The present measurements of the CFFs $\mathcal{E}$ and $\tilde{\mathcal{E}}$ therefore provide constraints on the quark momentum distribution support of the corresponding form factors within this $x_B$ range.

The present measurements will be complemented in this same general kinematic range in the near future by measurements in JLab Halls B and C, and longitudinally polarized proton measurements and neutron DVCS measurements in JLab Hall B. These measurements therefore demonstrate that the full extraction of experimental Compton form factors is within reach.

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